

Where are we in understanding parton distributions from the first principles?

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Fourth Lecture at RIKEN Center for Computational
Science, Kobe

10/21/2024

EIC + LaMET

The timing is just right to tackle the
problem of hadron and nuclear
structures.

LaMET

- Computing quasi-PDF with equal time quark bilinear matrix elements for proton states with large momenta

$$\tilde{q}(x, \mu^2, P^z) = \int \frac{dz}{4\pi} e^{-ixzP^z} \langle P | \bar{\psi}(0) \lambda \cdot \gamma \Gamma \psi(z\lambda) | P \rangle$$
$$\lambda^\mu = (0, 0, 0, 1)$$

- Factorization theorem: analogous to HQET: need power corrections & matching

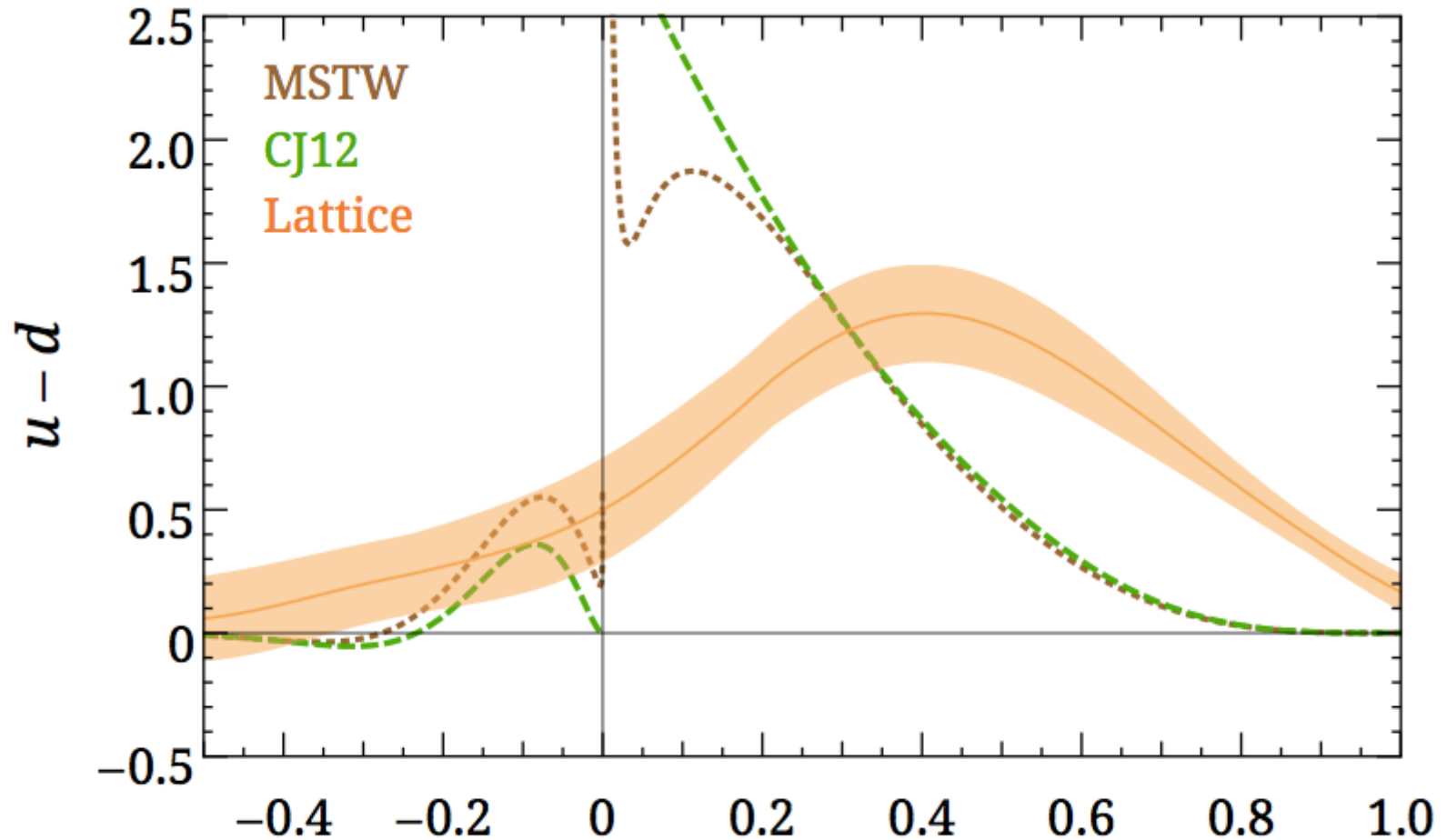
UV, PQCD

$$\tilde{q}(x, \Lambda, P_z) = \int \frac{dy}{|y|} Z\left(\frac{x}{y}, \frac{\mu}{P_z}, \frac{\Lambda}{P_z}\right) q(y, \mu) + \mathcal{O}\left(\frac{\Lambda_{\text{QCD}}^2}{P_z^2}, \frac{M^2}{P_z^2}\right) + \dots$$

LaMET 1.0

Proton Unpolarized PDF

LP3 (1402.1462)



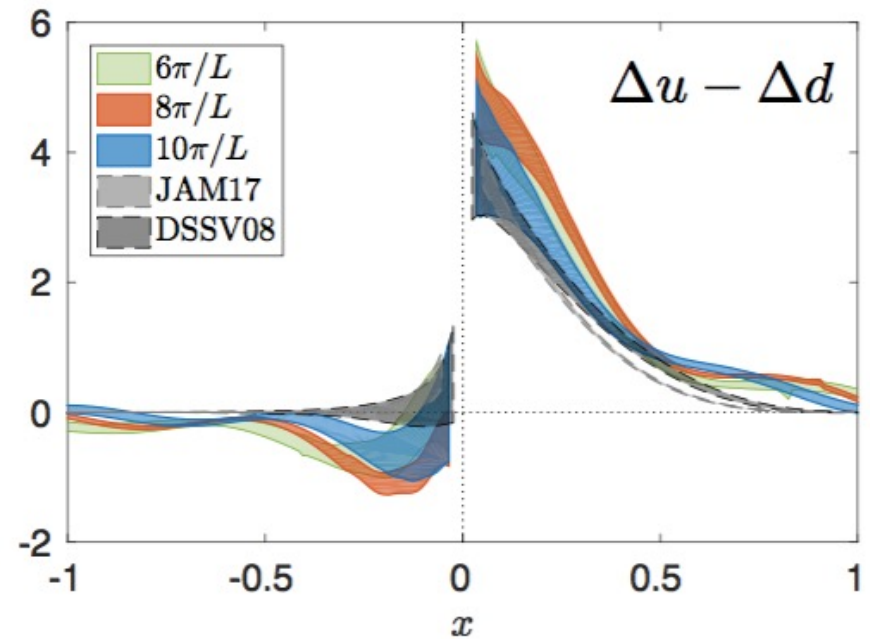
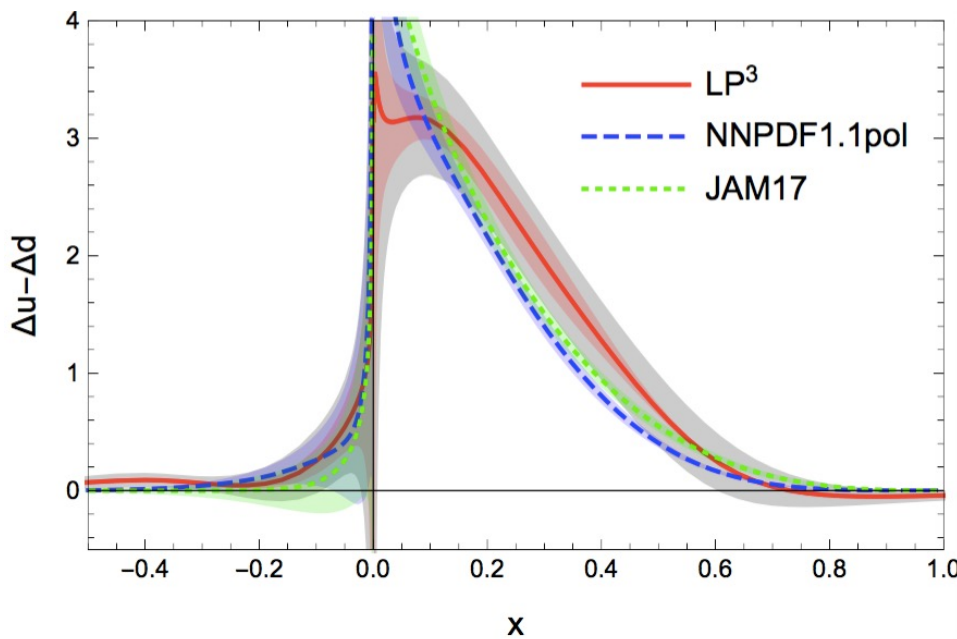
$$q(-x) = -\bar{q}(x)$$

power corrections: JWC, Cohen, Ji,
X Lin, Zhang

matching: Xiong, Ji, Zhang, Zhao

LaMET 2.0

Proton Helicity PDF



LP3(1807.07431,PRL)

ETMC(1803.02685,PRL)

Momentum smearing: Bali, Lang, Musch, Schafer

Factorization: Ma, Qiu; Izubuchi, Ji, Jin, Stewart, Zhao

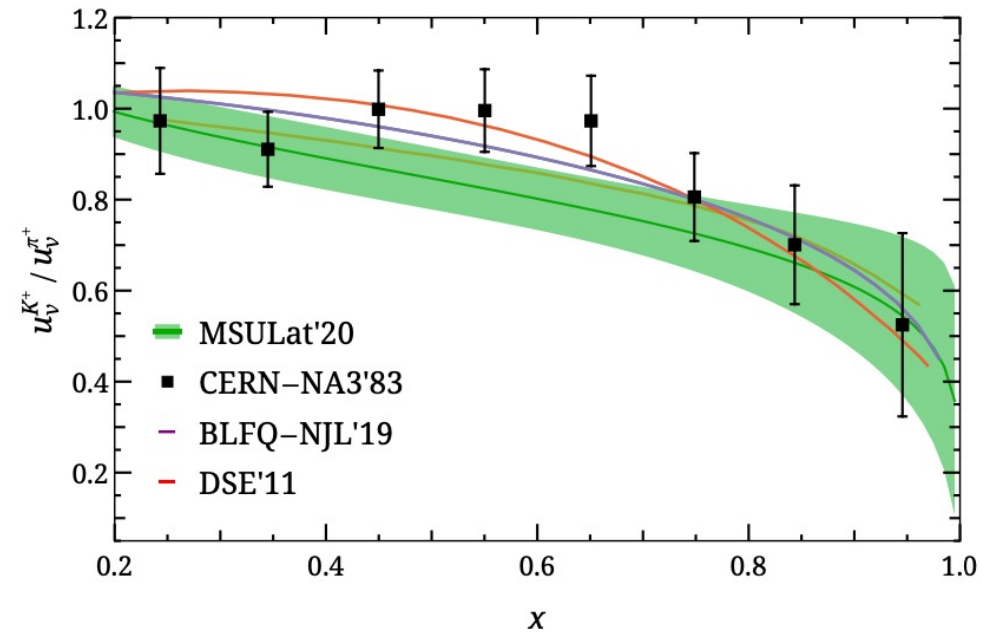
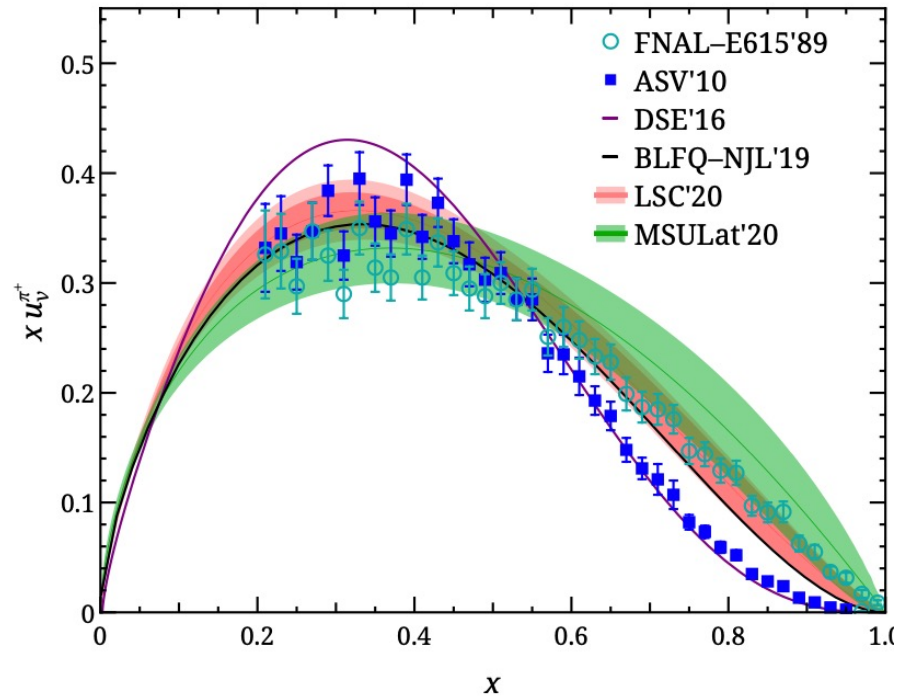
Wilson line mass subtraction: JWC, Ji, Zhang

LPT: Ishikawa, Ma, Qiu, Yoshida; Xiong, Luu, Meissner; Constantinou et al.

Multiplicative renormalizability: Ji, Zhang, Zhao

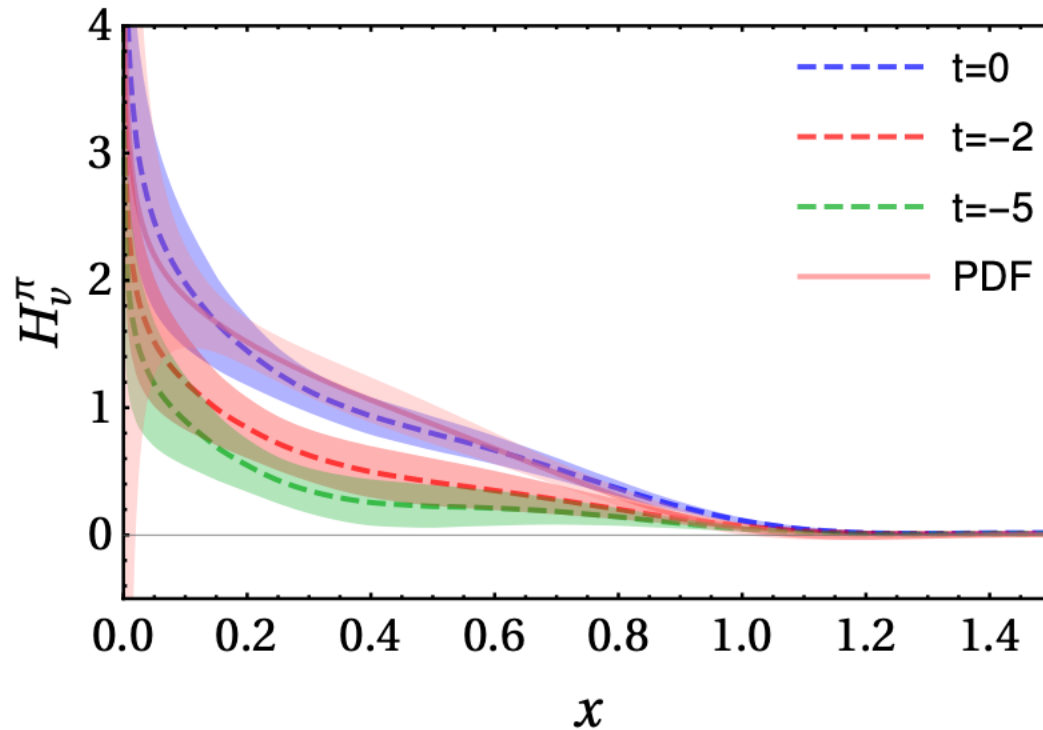
NPR: RI/MOM: Yong, Stewart; Constantinou et al.; **Ratio:** Radyushkin

Meson Valence Quark Distributions



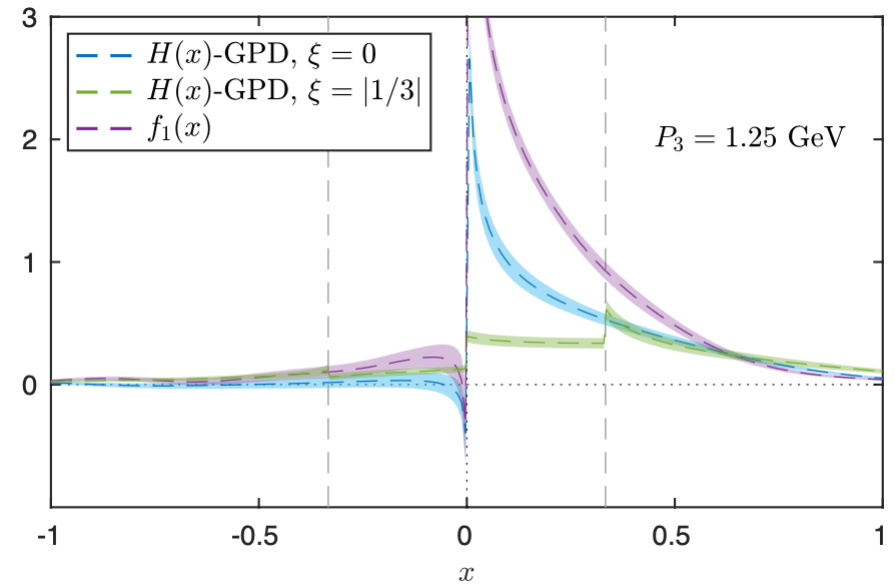
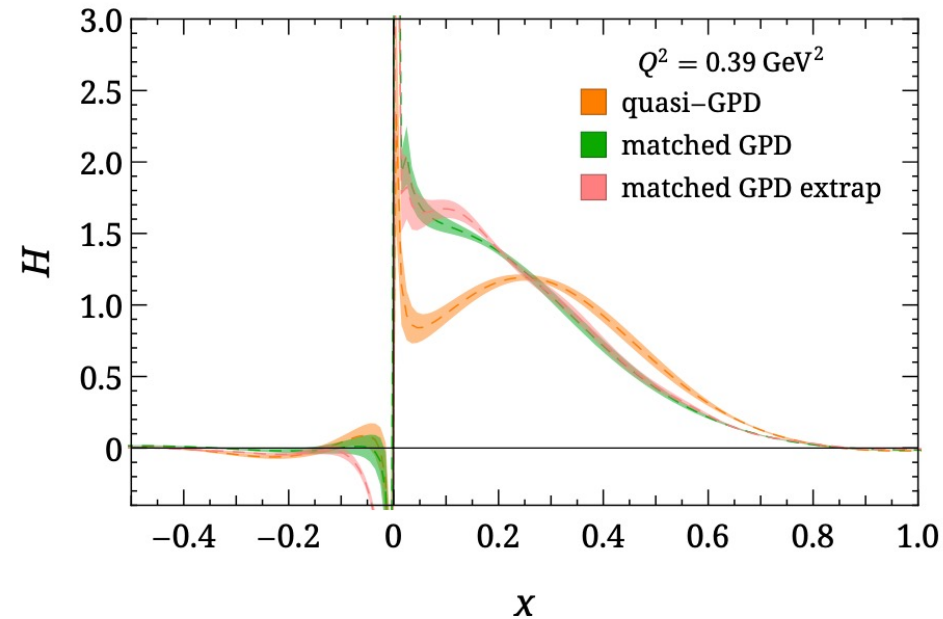
HW Lin, JWC, Z Fan, JH Zhang, R Zhang (2003.14128)

Pion Skewless Valance GPD



JWC, HW Lin, JH Zhang (1904.12376)

Nucleon GPD at Physical Pion Mass

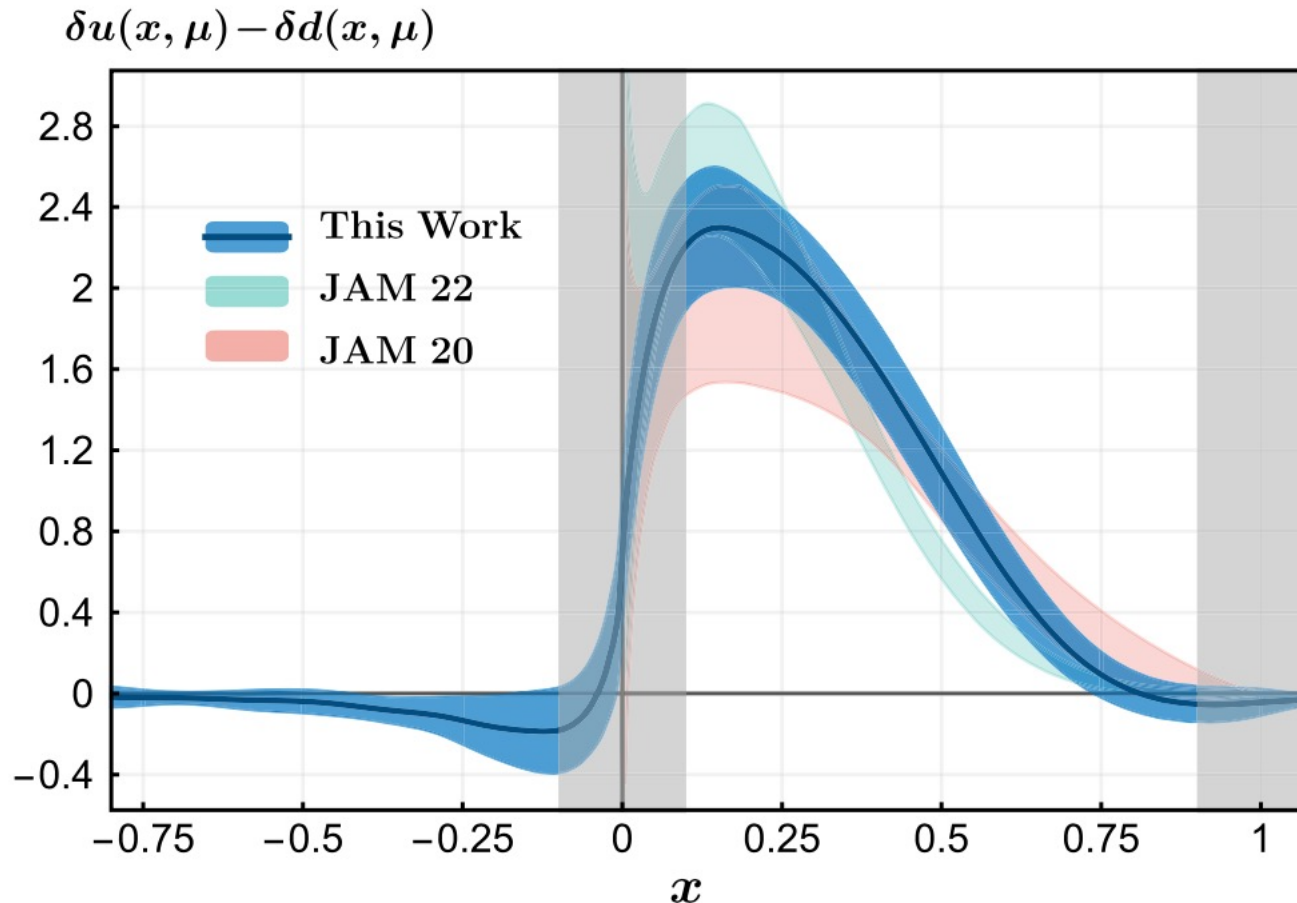


HW Lin (2008.12474, PRL)
 $M_{\pi} = 140 \text{ MeV}$

ETMC (2008.10573, PRL)
 $M_{\pi} = 260 \text{ MeV}$

LaMET 3.0

Proton Transversity PDF in the Continuum and Physical Mass Limit

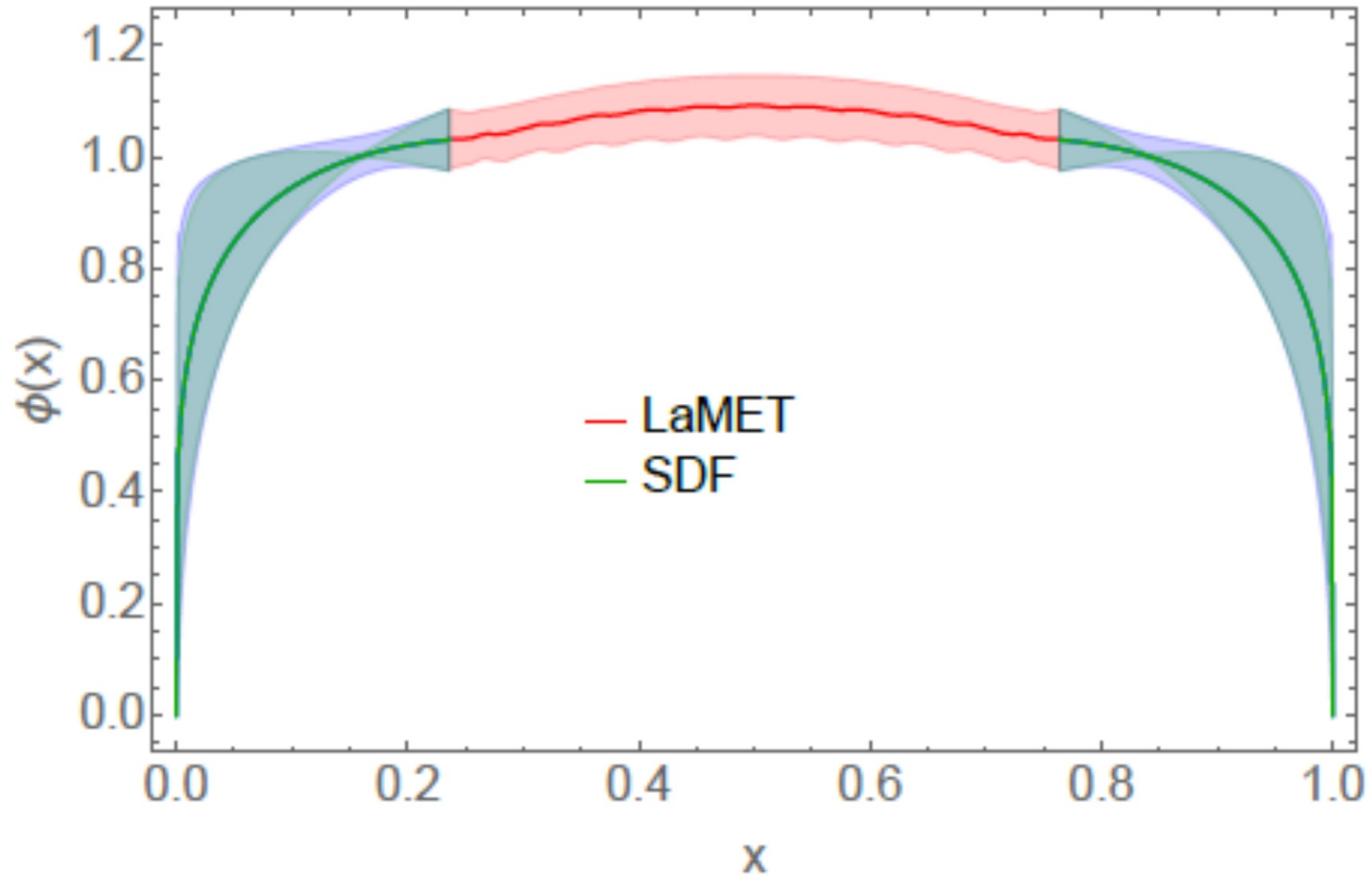


Yao, Walter, JWC, et al. (LPC), PRL 2023

Renormalon: Braun, Vladimirov, Zhang

Hybrid renormalization: Ji, Liu, Schäfer, Wang, Yang, Zhang, Zhao

Pion Distribution Amplitude

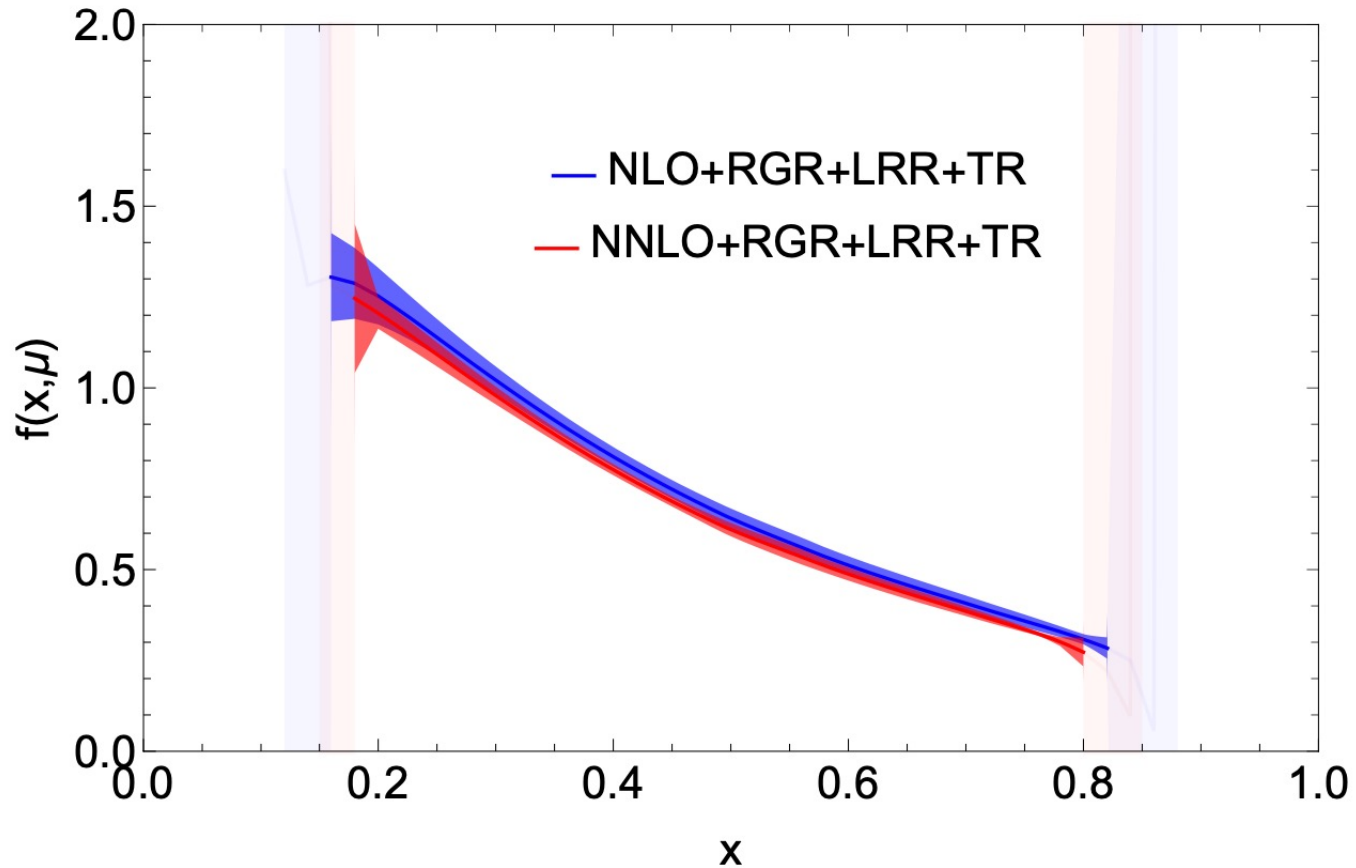


J. Holligan et al 2301.10372

Most recent developments

- Precision frontier: NNLO matching, Resummations, no Wilson line, Lanczos ([D. Hackett, M. Wagman](#)), high precision gauge fixing ([YB Yang](#))
- Higher dimensional frontier: TMD, GPD
- Flavor frontier? gluon, $u+d$, s , c , $b(?)$

Resummations



Xiangdong Ji, Yizhuang Liu, Yushan Su, Rui Zhang (2410.12910)

NNLO kernel: ZY Li, YQ Ma, JW.Qiu; LB Chen, W Wang, R Zhu

Resummations: **RGR**: $\ln(x)$ powers; **TR**: $\ln(1-x)$ powers; **LRR**: leading renormalon

Nuclear Parton Distributions?

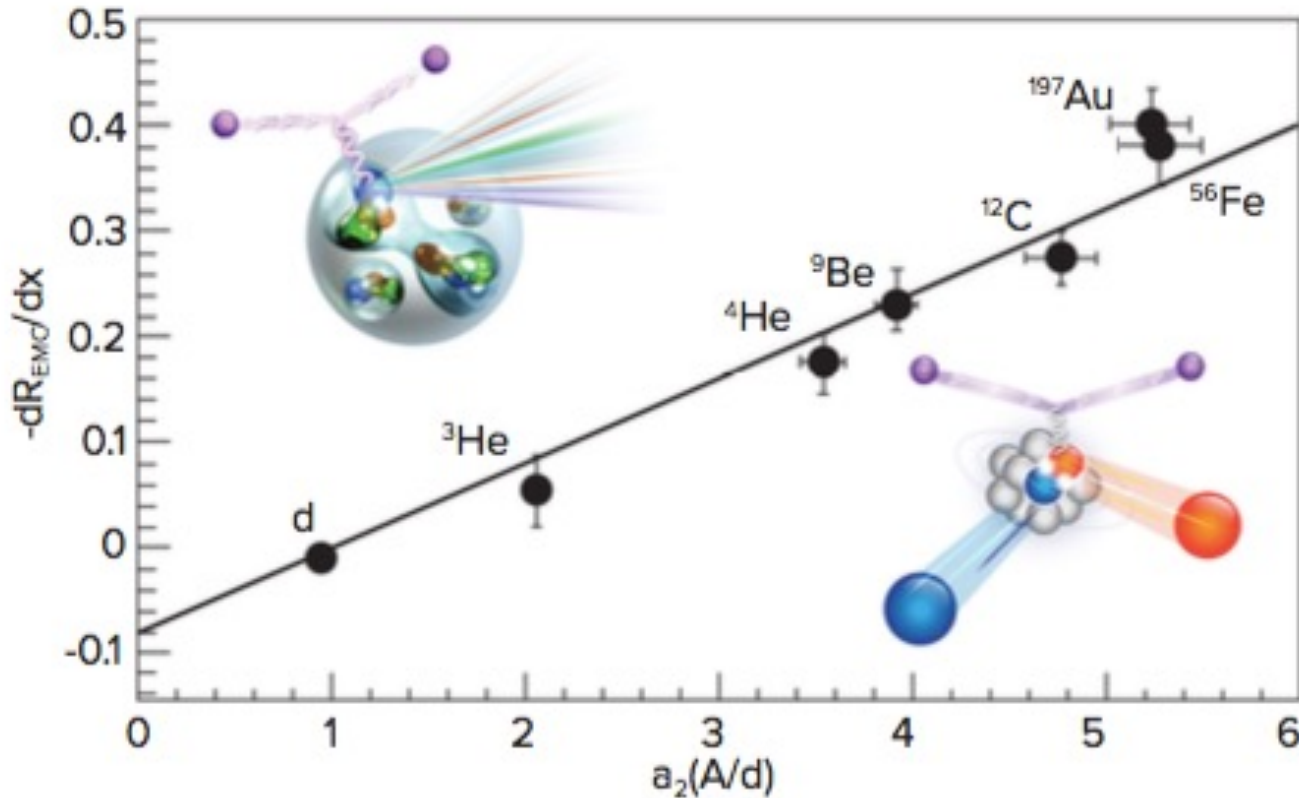
EMC/SRC Connections in EFT & QCD

w/ William Detmold, hep-ph/0412119, Phys.Lett. B625 (2005) 165

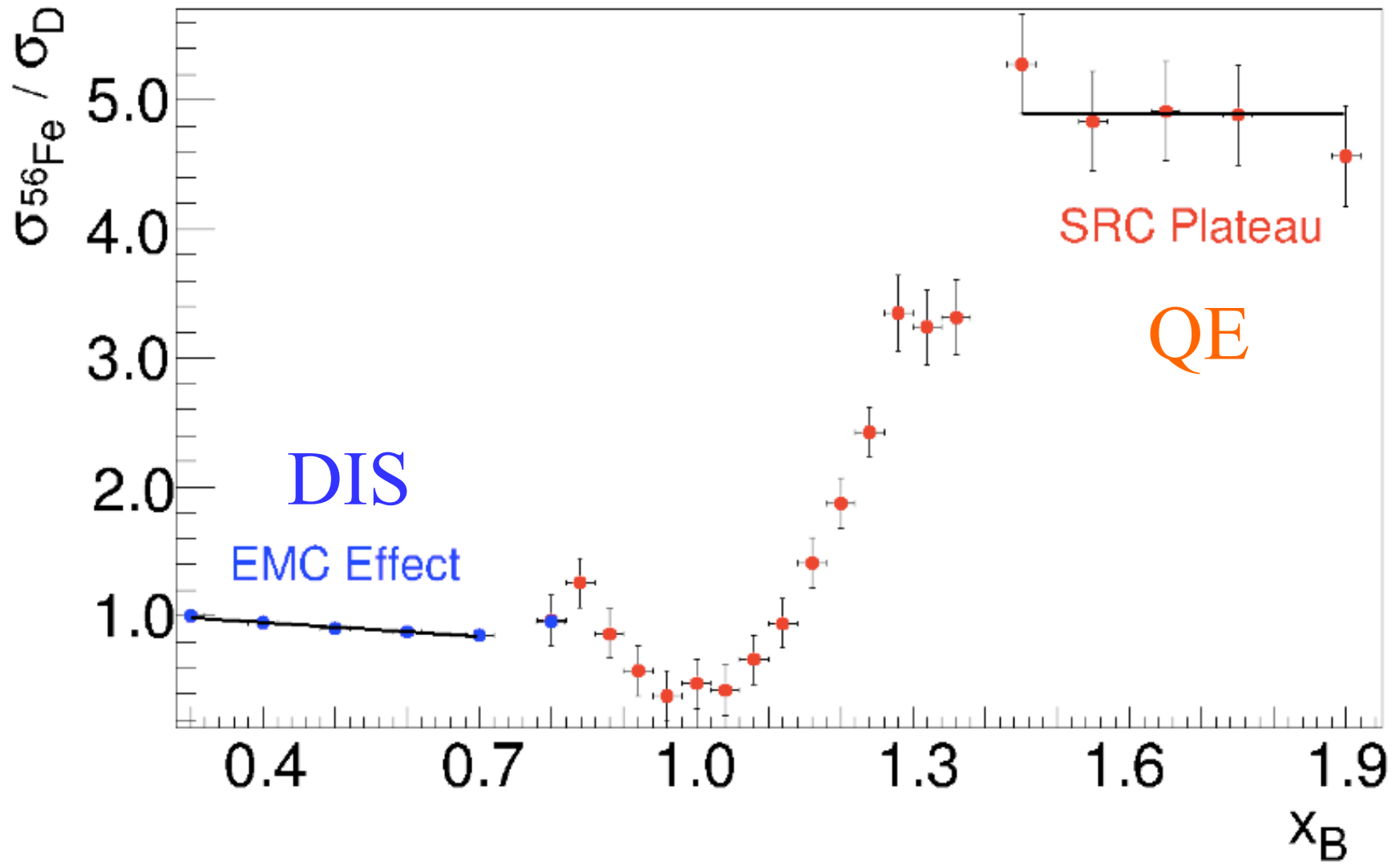
w/ William Detmold, Joel E. Lynn, Achim Schwenk, 1607.03065, Phys. Rev. Lett. 119 (2017) 262502

w/ Lynn, Lonardoni, Carlson, Detmold, Gandolfi, Schwenk, J.Phys.G 47 (2020) 045109

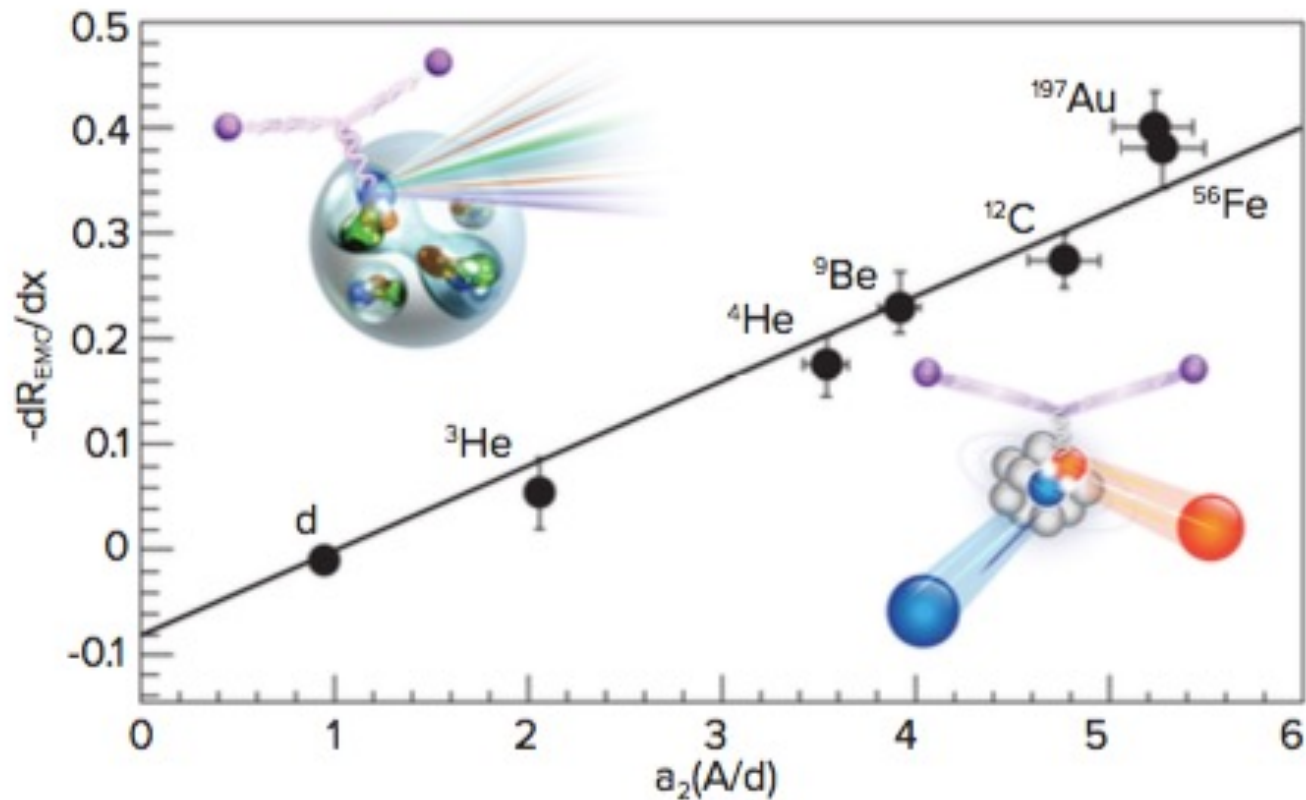
An Astonishing Empirical Result!



Weinstein et al., Phys. Rev. Lett. 106, 052301 (2011)



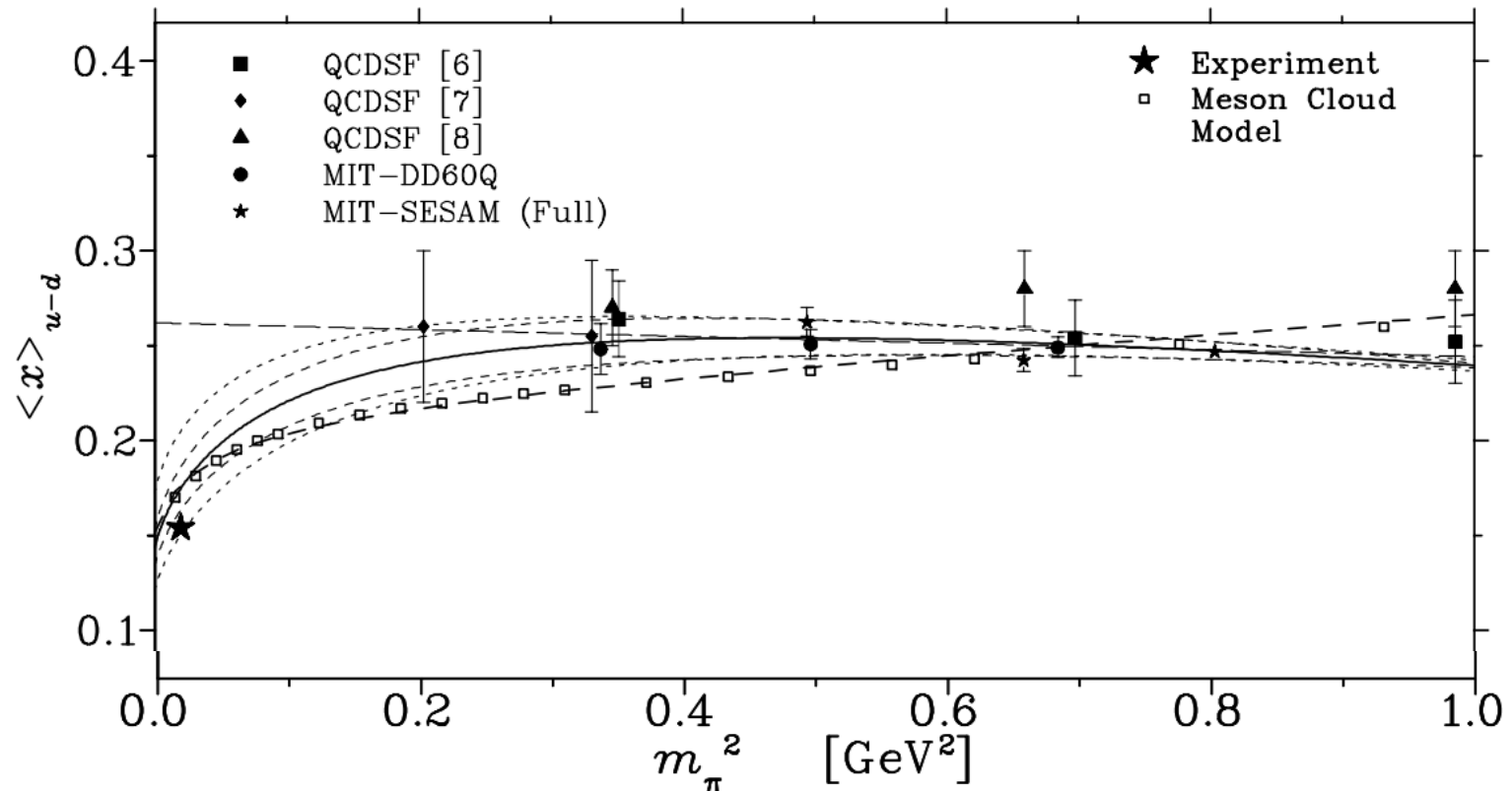
Promises from EFT



- EMC-SRC linear relation reproduced
- Some a_2 reproduced ab initio
- Remaining problem: EMC slope from LQCD (only need deuteron)

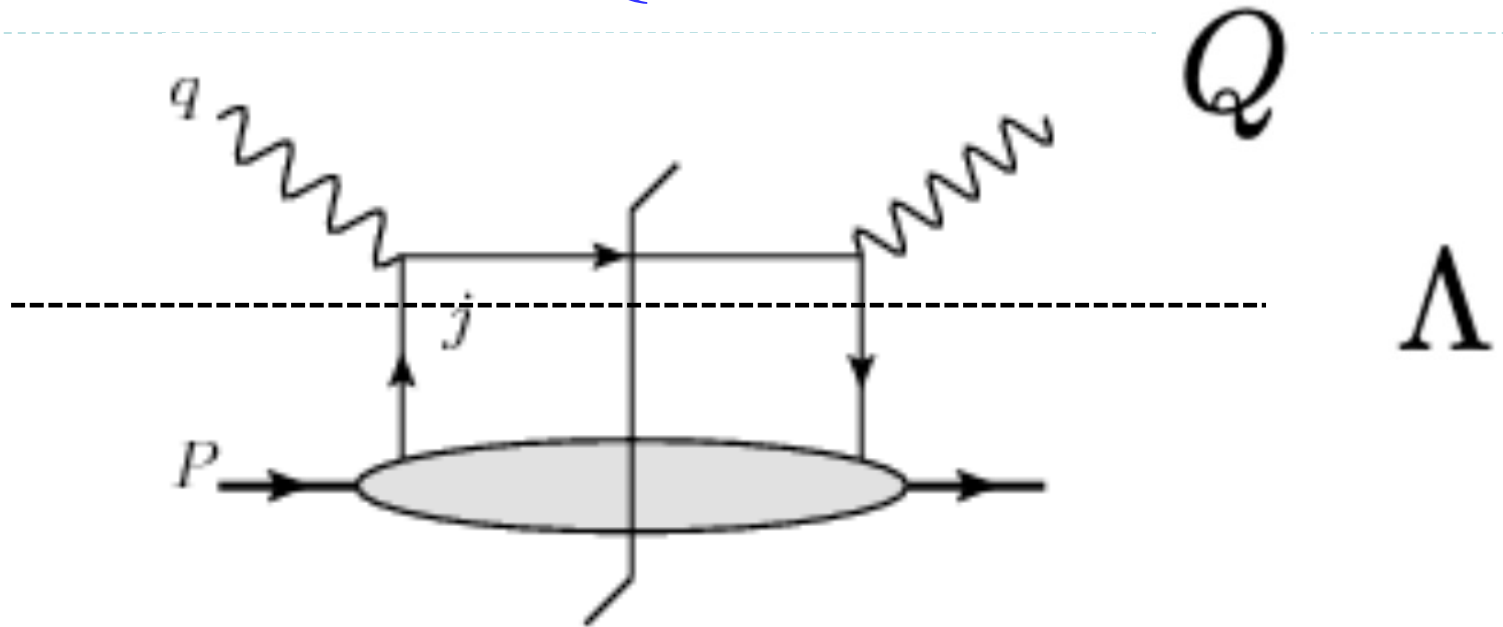
No free parameters involved!

Lattice Moments (Local Twist-2 Matrix Elements) in LQCD



Detmold, Melnitchouk, Negele, Renner, Thomas,
Phys.Rev.Lett.87:172001,2001

Parton Distribution Function (PDF) in QCD



The struck parton moves on a light cone at the leading order in the twist-expansion:

$$\Lambda/Q \ll 1$$

Further Separate the Pion Mass Scale

$$Q \gg \Lambda \gg P \sim m_\pi$$

- Double expansion:

Twist expansion in Λ/Q (PQCD)

Chiral expansion in $\epsilon \sim P/\Lambda \sim 0.2 - 0.3$
(ChPT)

JWC, Ji, Phys. Lett. B523 (2001) 107

Phys.Rev.Lett. 87 (2001) 152002

Phys.Rev.Lett. 88 (2002) 052003

JWC, Stewart, Phys.Rev.Lett. 92 (2004) 202001

Arndt, Savage, Nucl.Phys. A697 (2002) 429

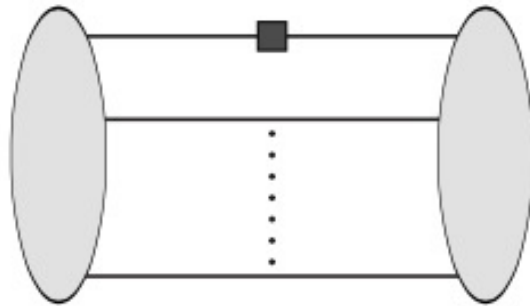
EMC Effect in EFT (JWC, Detmold, 2005)

Twist-2 operator matching (isoscalar):

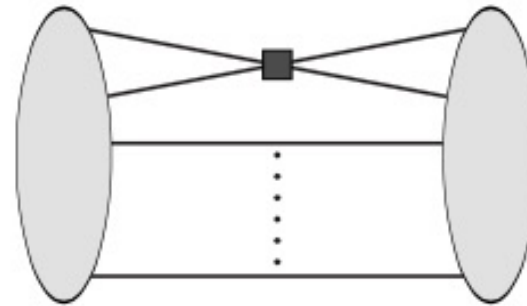
$$\mathcal{O}^{\mu_0 \cdots \mu_n} = \bar{q} \gamma^{(\mu_0} i D^{\mu_1} \cdots i D^{\mu_n)} q,$$

$$\begin{aligned} \mathcal{O}^{\mu_0 \cdots \mu_n} \rightarrow & \langle x^n \rangle_N M^n v^{(\mu_0} \cdots v^{\mu_n)} N^\dagger N [1 + \alpha_n N^\dagger N] \\ & + \langle x^n \rangle_\pi \pi^\alpha i \partial^{(\mu_0} \cdots i \partial^{\mu_n)} \pi^\alpha + \dots, \end{aligned}$$

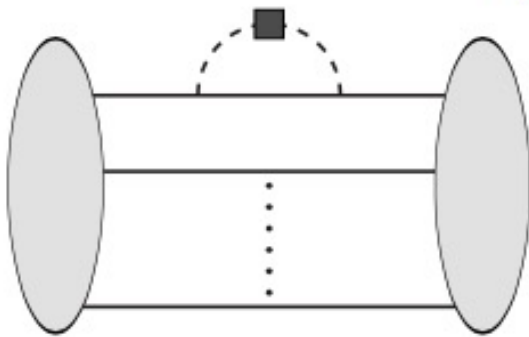
Using large N_c counting



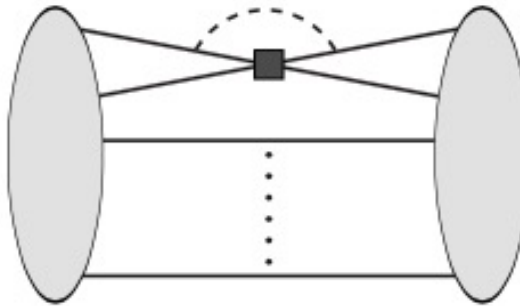
(a)



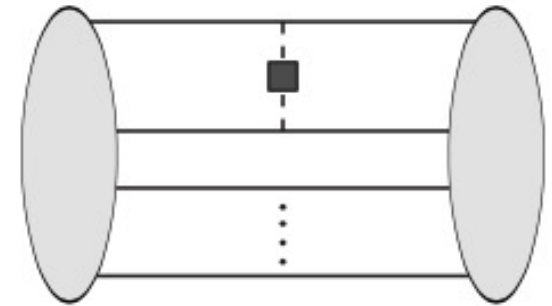
(b)



(c)



(d)



(e)

$$g_2(A, \Lambda) = \frac{1}{A} \langle A | (N^\dagger N)^2 | A \rangle_\Lambda,$$

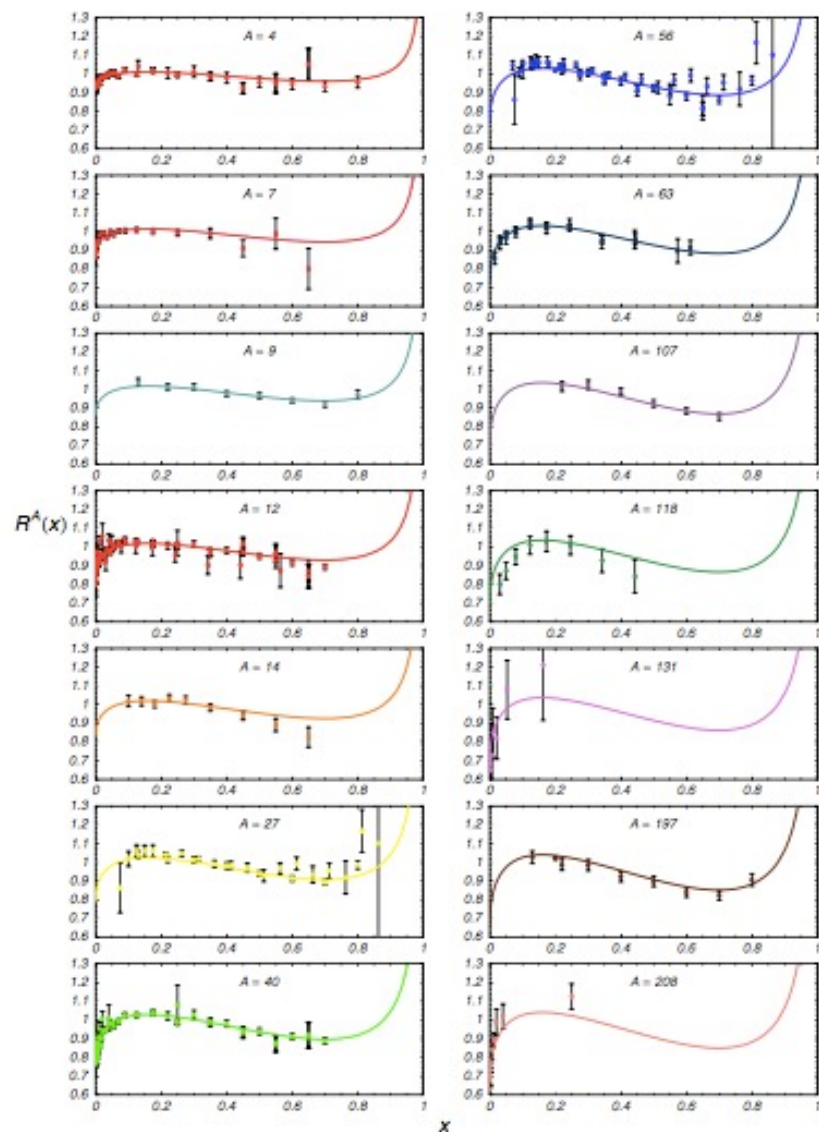
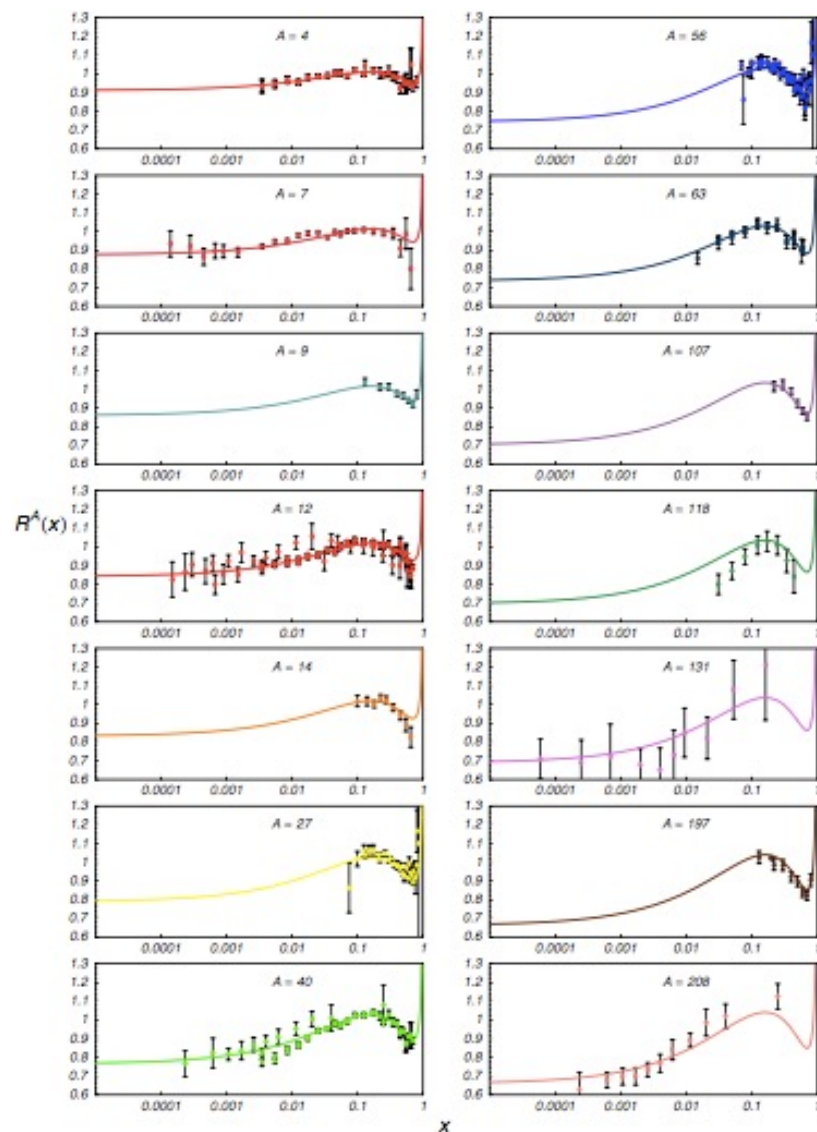
Factorization
Implies prediction power!

$$q_A(x)/A = q_N(x) + g_2(A, \Lambda) \tilde{q}_2(x, \Lambda)$$

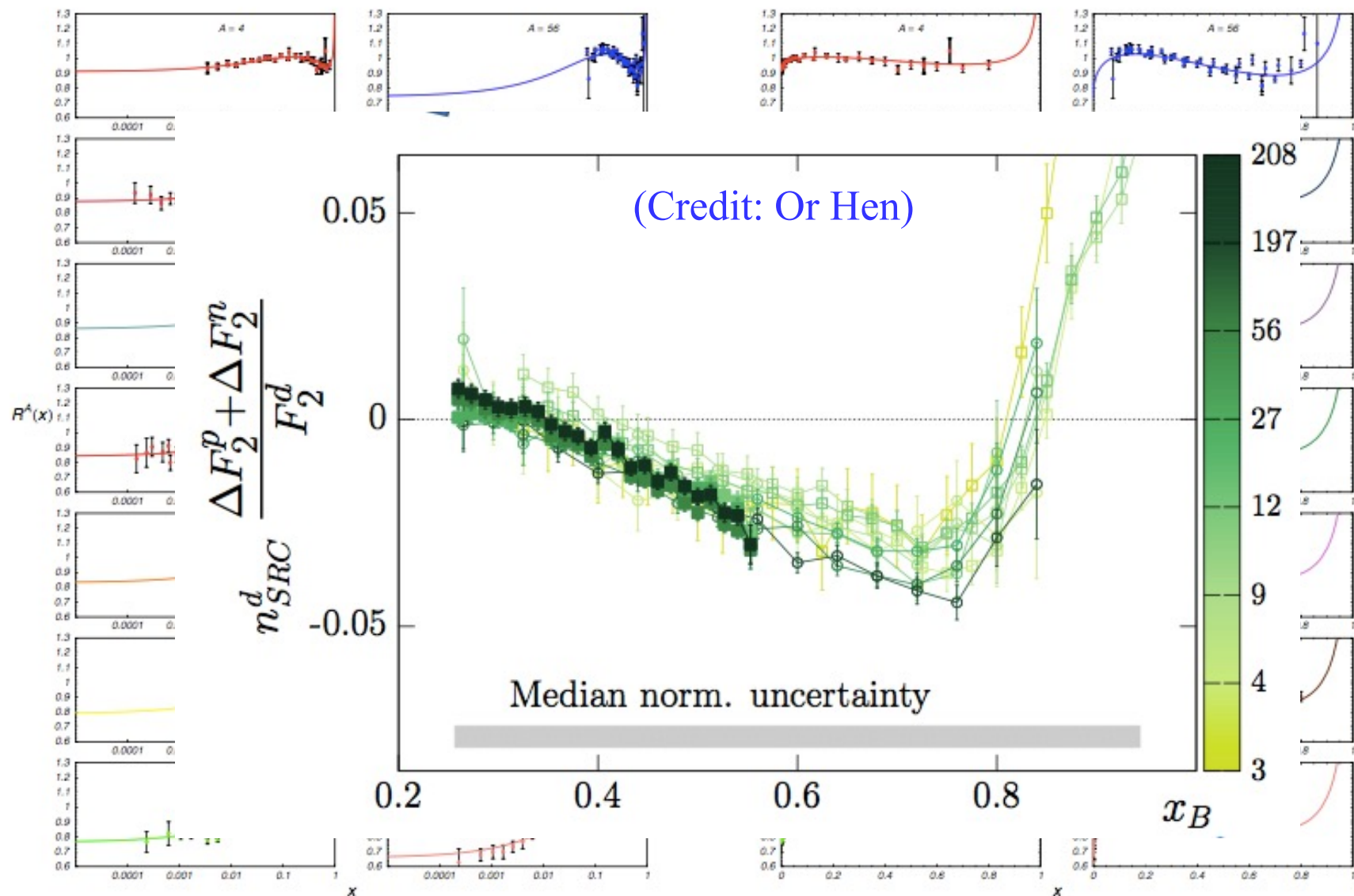
1-body op.
2-body op.
determined by deuteron

EFT predicts EMC $R_A(x) - 1 = f(A)\phi(x)$

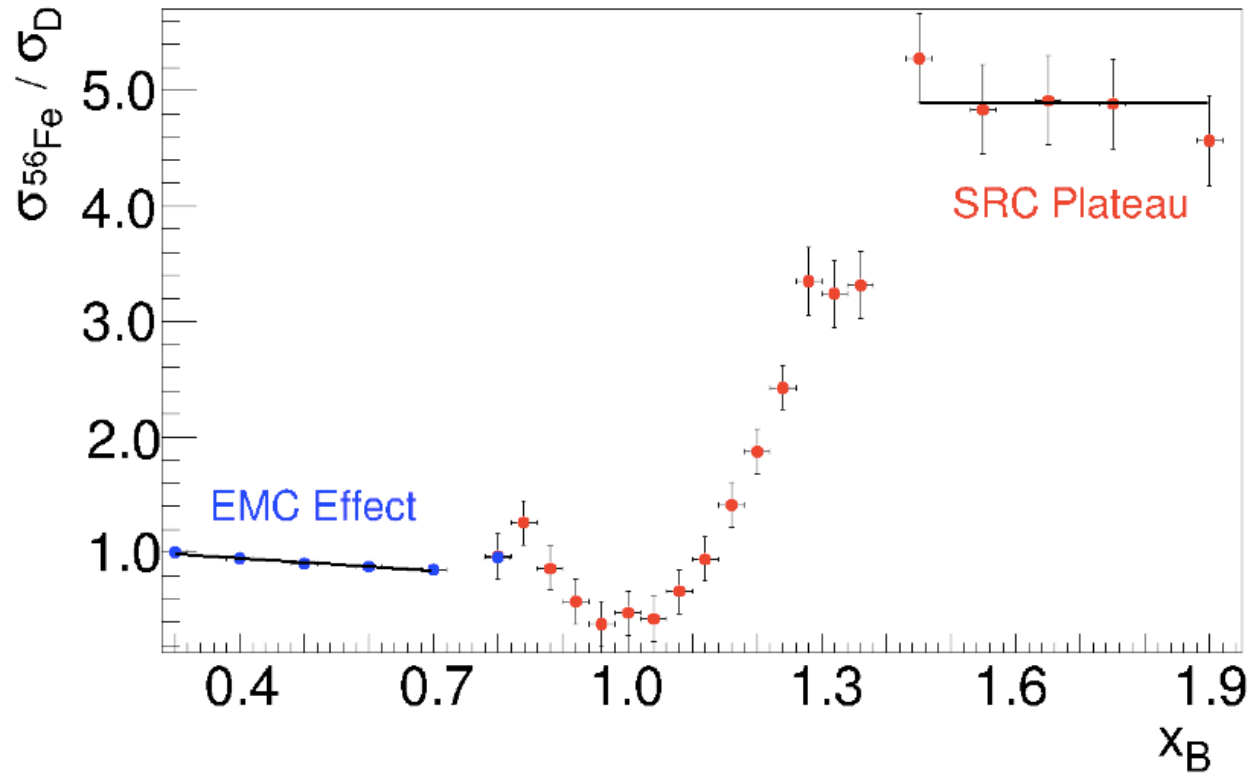
EFT predicts EMC $R_A(x) - 1 = f(A)\phi(x)$



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SRC scaling factor (same in QE)



$$q_A(x)/A = q_N(x) + g_2(A, \Lambda) \tilde{q}_2(x, \Lambda) \quad q_N(x > 1) = 0$$

Indept of scheme
& scale!

$$a_2(A, x > 1) = \frac{2q_A(x)}{Aq_d(x)} = \frac{g_2(A, \Lambda) \tilde{q}_2(x, \Lambda)}{g_2(2, \Lambda) \tilde{q}_2(x, \Lambda)} = \frac{g_2(A, \Lambda)}{g_2(2, \Lambda)}$$

a_2 : scheme and scale independent

Ratio of **LOW** energy quantities:

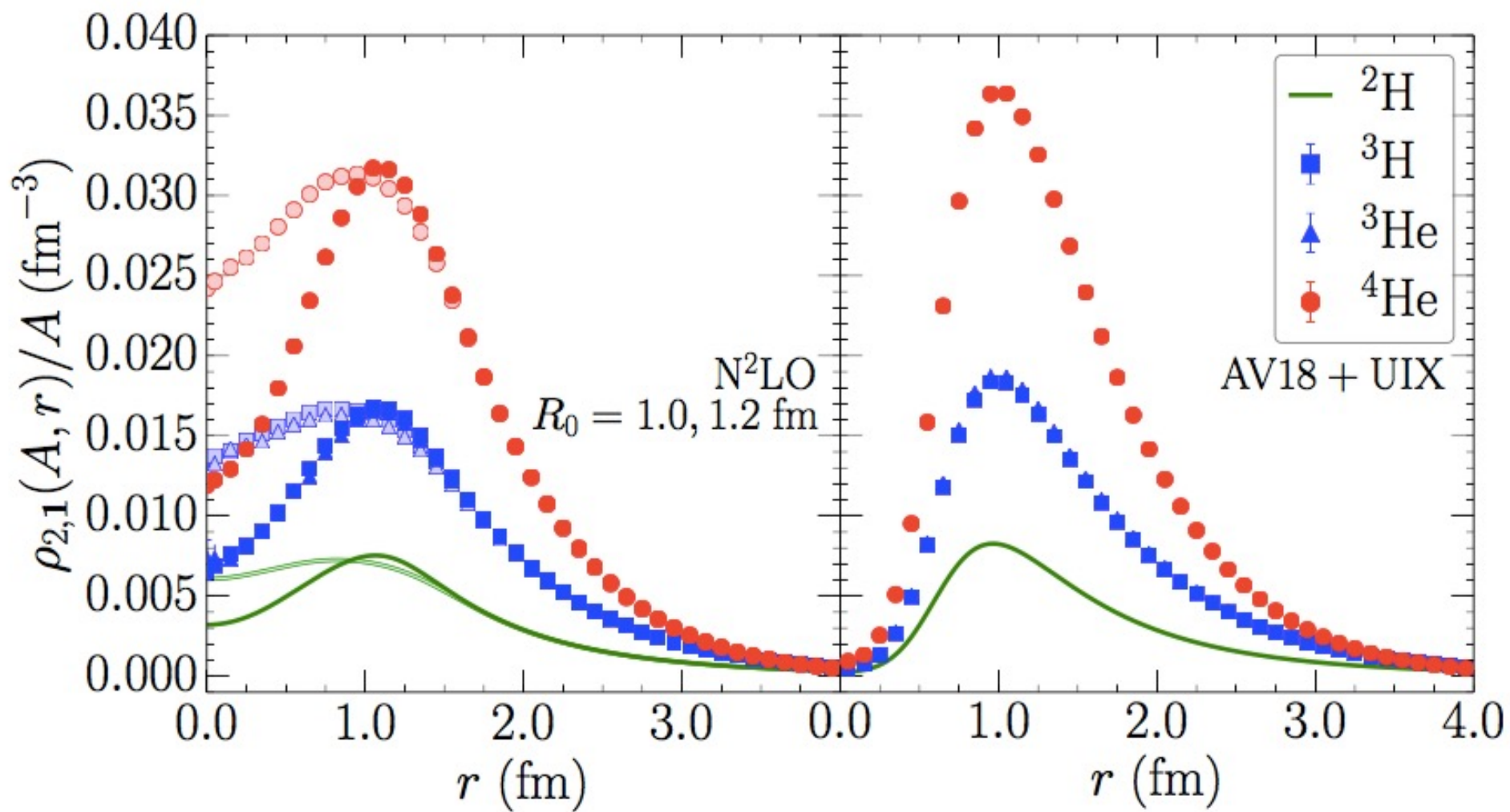
$$a_2(A, x > 1) = \frac{g_2(A, \Lambda)}{g_2(2, \Lambda)}.$$

$$g_2(A, \Lambda) = \frac{1}{A} \langle A | (N^\dagger N)^2 | A \rangle_\Lambda,$$

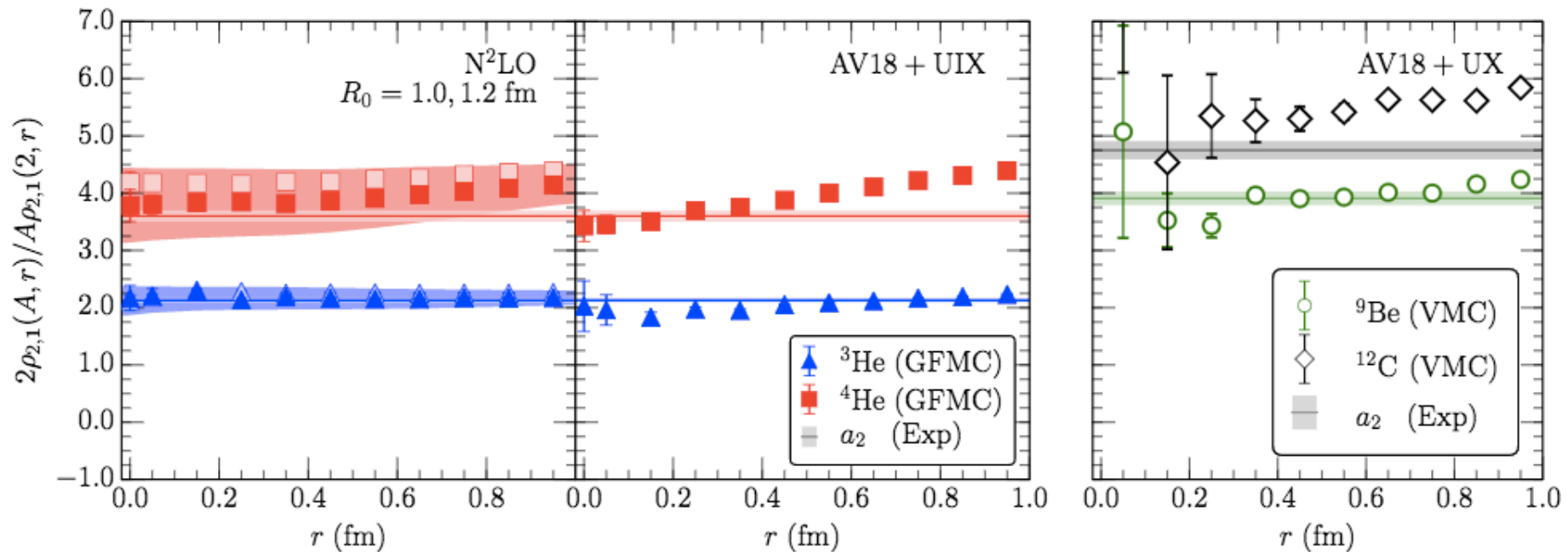
$$= \rho_{2,1}(A, r = 0)/A$$

$$\rho_{2,1}(A, r) = \frac{1}{4\pi r^2} \left\langle \Psi_0 \left| \sum_{i < j}^A \delta(r - |\mathbf{r}_i - \mathbf{r}_j|) \right| \Psi_0 \right\rangle$$

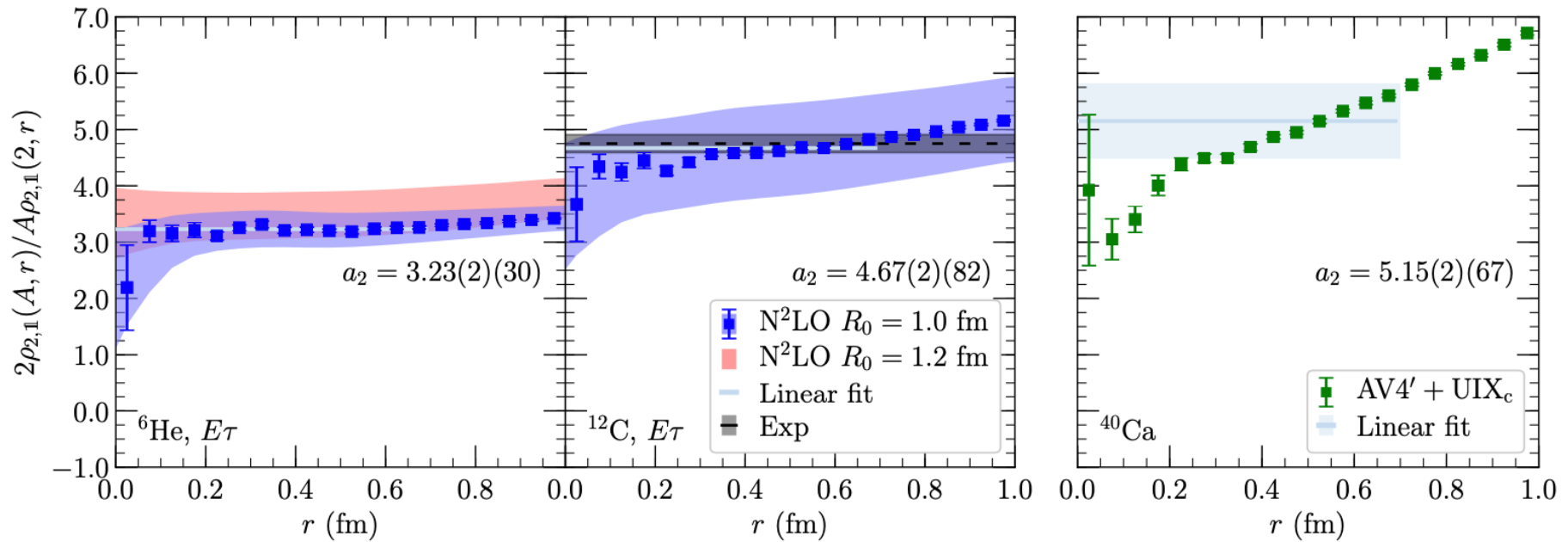
$\rho_{2,1}(A, r)/A$: scheme and scale DEPENDENT



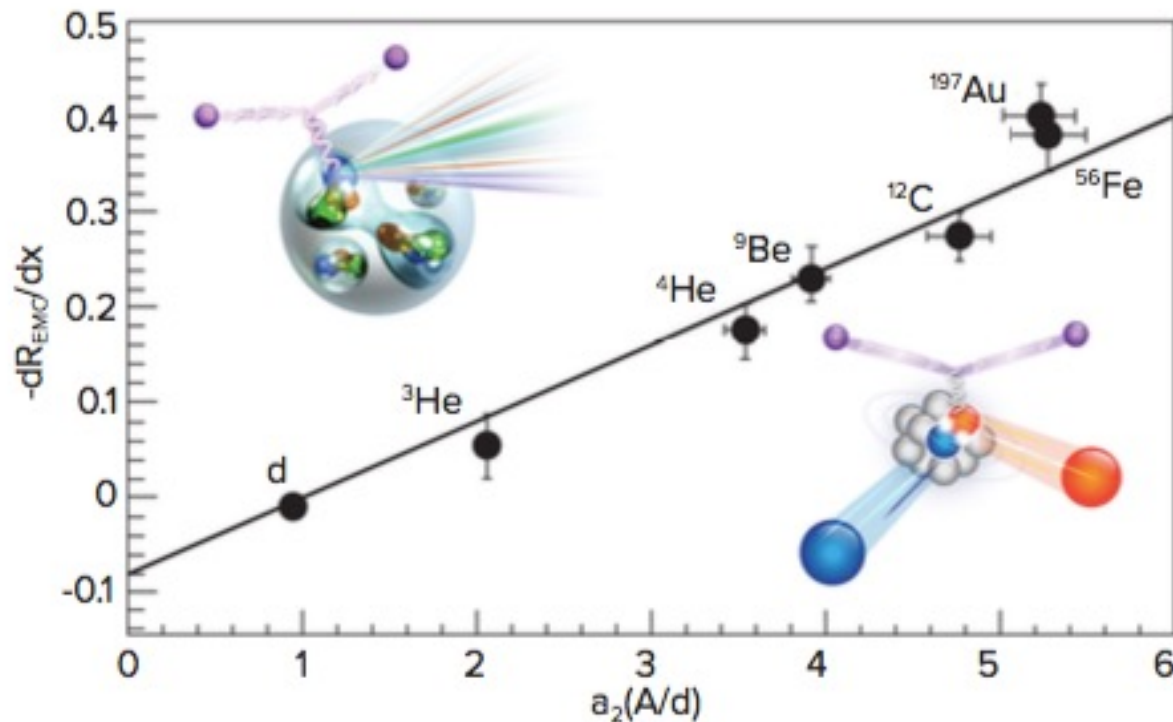
a_2 : scheme and scale independent



a_2 : scheme and scale independent



Towards a parameter free understanding



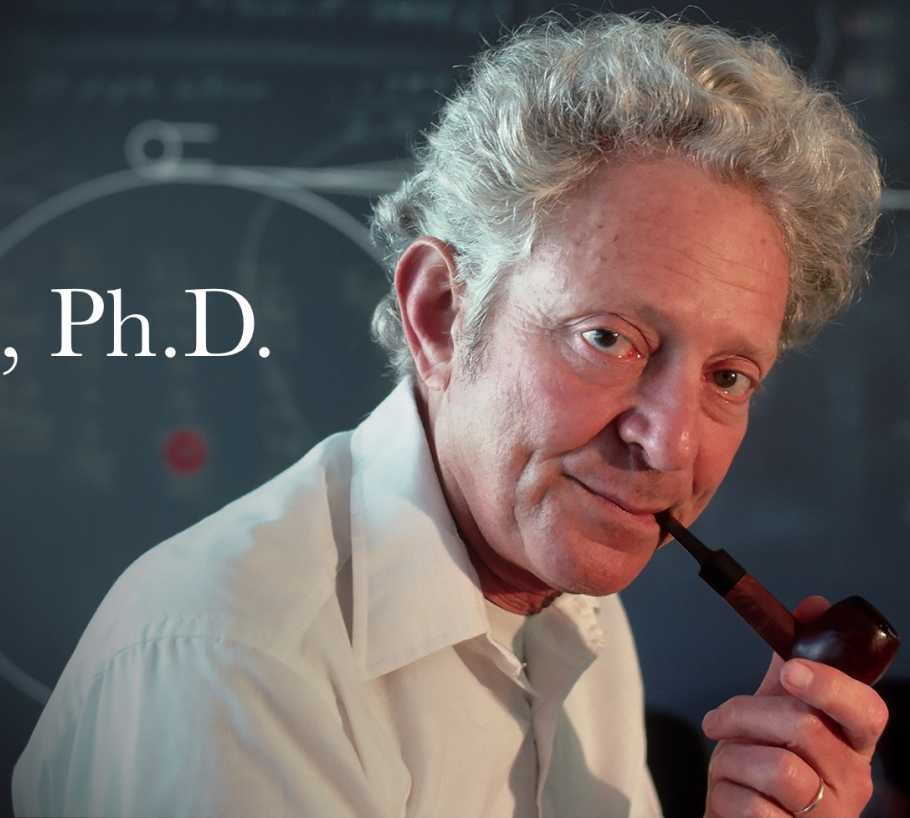
- EMC-SRC linear relation reproduced
- Some a_2 reproduced ab initio
 - Remaining problem: EMC slope from LQCD
(only need deuteron) $\Rightarrow$ LaMET!

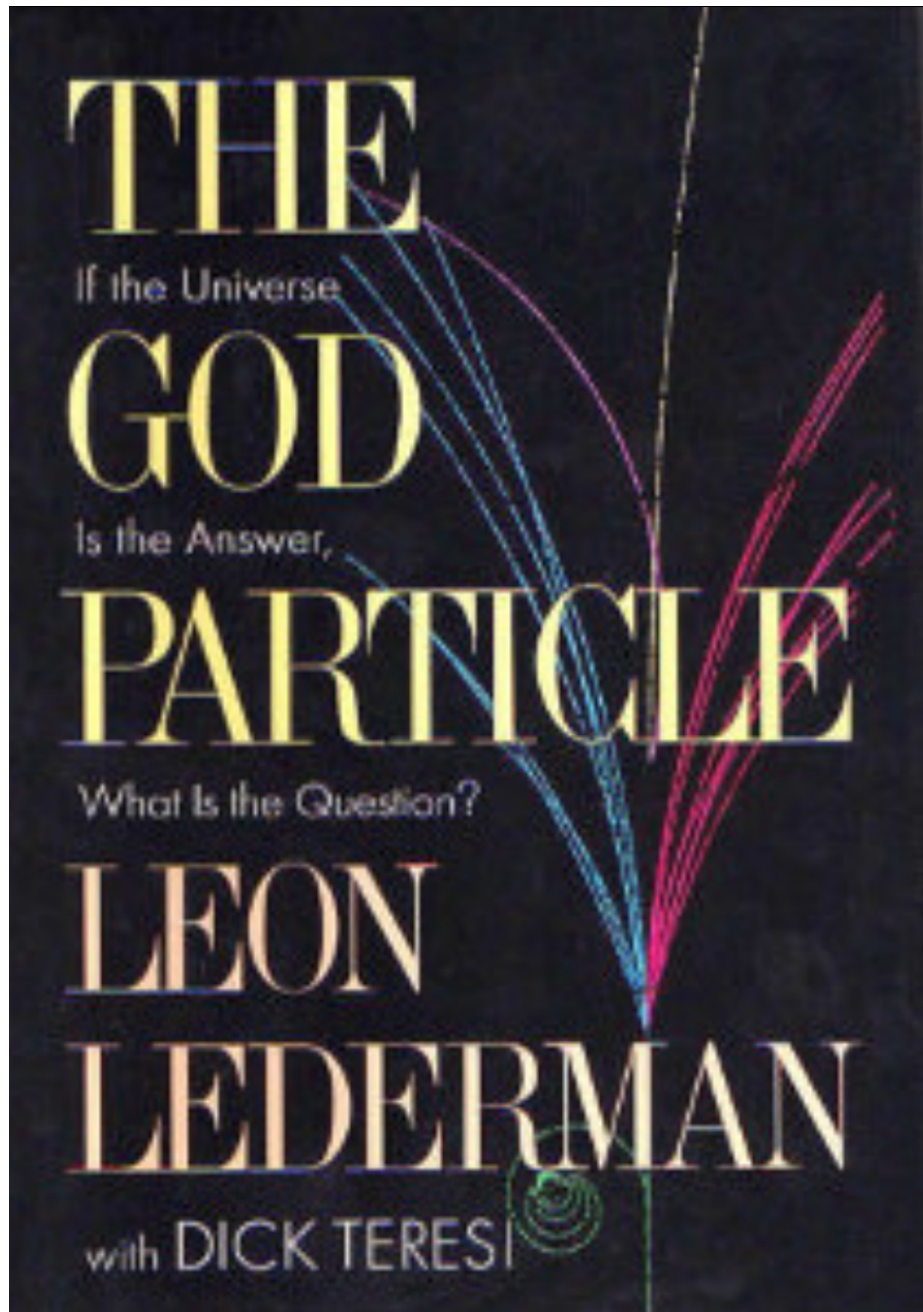
- EMC-SRC linear relation: a simple and elegant empirical result, might one day be explained in first principles (QCD and its EFT) with no free parameter!
- Possible applications:
 - (a) ν -A inclusive scattering for long baseline exp.
 - (b) 3D imagining of nuclear PDFs?

< ALL ACHIEVERS

Leon Lederman, Ph.D.

.....
Nobel Prize in Physics





The God Particle:

If the Universe Is
the Answer,

What Is
the Question?

An Ultimate Question in Science

Life = Physical Laws ?

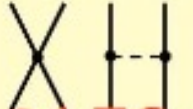
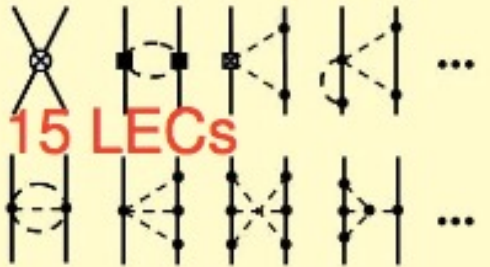
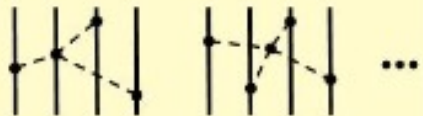
And We Are All in the Pursuit
towards Answering this Question!

Thank you very much!



Backup

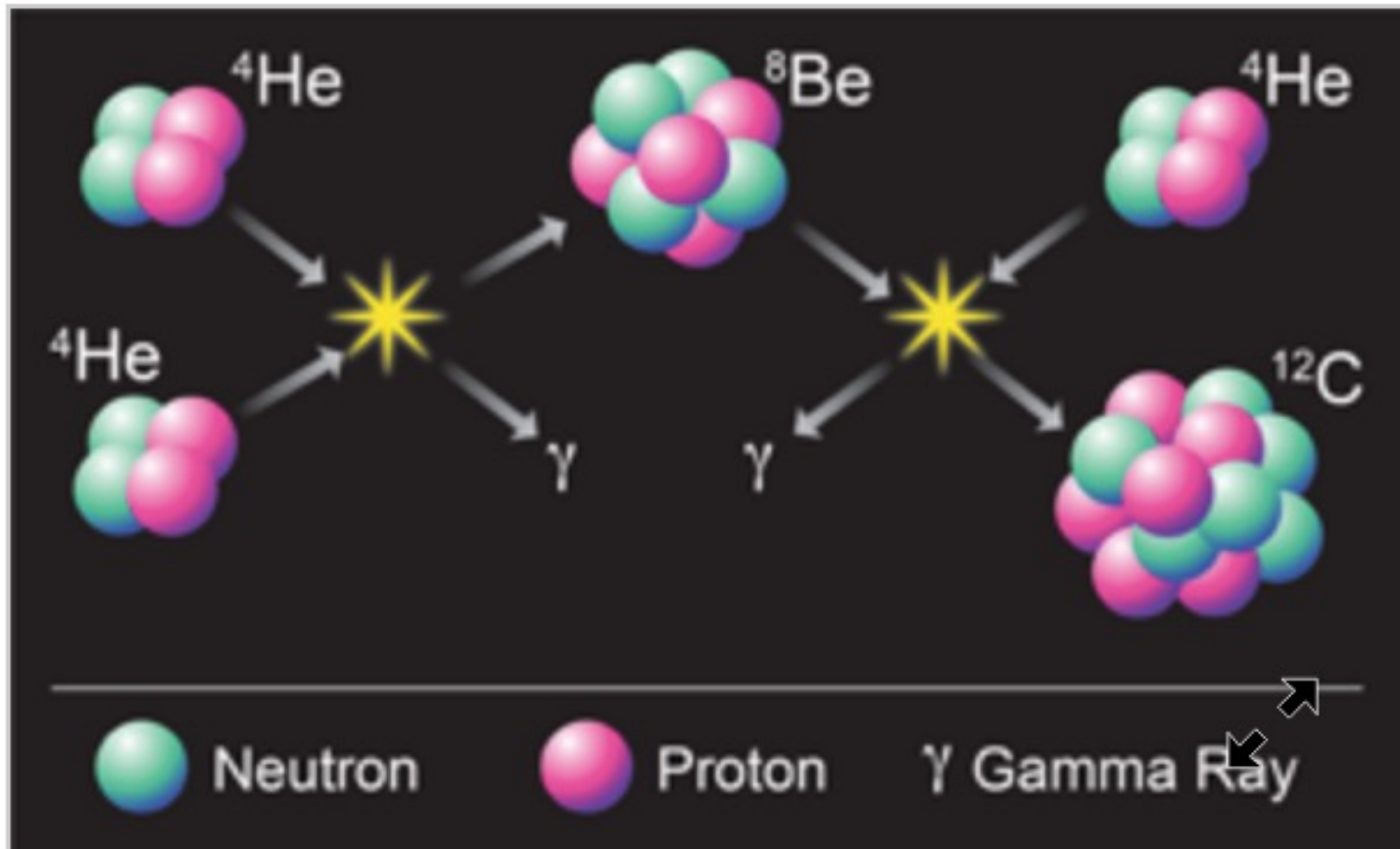
Applying ChPT to nuclear systems (Weinberg)

	Two-nucleon force	Three-nucleon force	Four-nucleon force
LO	 2 LECs	—	—
NLO	 7 LECs	—	—
N ² LO		 2 LECs	—
N ³ LO	 15 LECs		

Credit: U-G Meissner

Hoyle State Obtained

Epelbaum, Krebs, Lee, Meißner, Phys. Rev. Lett. 106, 192501 (2011)



Credit: Carin Cain

No Wilson Line

(Xiang Gao, Wei-Yang Liu, Yong Zhao)

Boosting brings the equal time correlator

$$\tilde{h}(z, P^z, \mu) = \frac{1}{2P^t} \langle P | \bar{\psi}(z) \gamma^t \psi(0) | P \rangle_{\vec{\nabla} \cdot \vec{A} = 0}$$

in Coulomb gauge w/o Wilson line towards the light cone correlator

$$h(\lambda, \mu) = \frac{1}{2P^+} \langle P | \bar{\psi}(\xi^-) W(\xi^-, 0) \gamma^+ \psi(0) | P \rangle$$

w/ Wilson line