

Chimera baryon spectrum in the $Sp(4)$ gauge theory

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The collaboration



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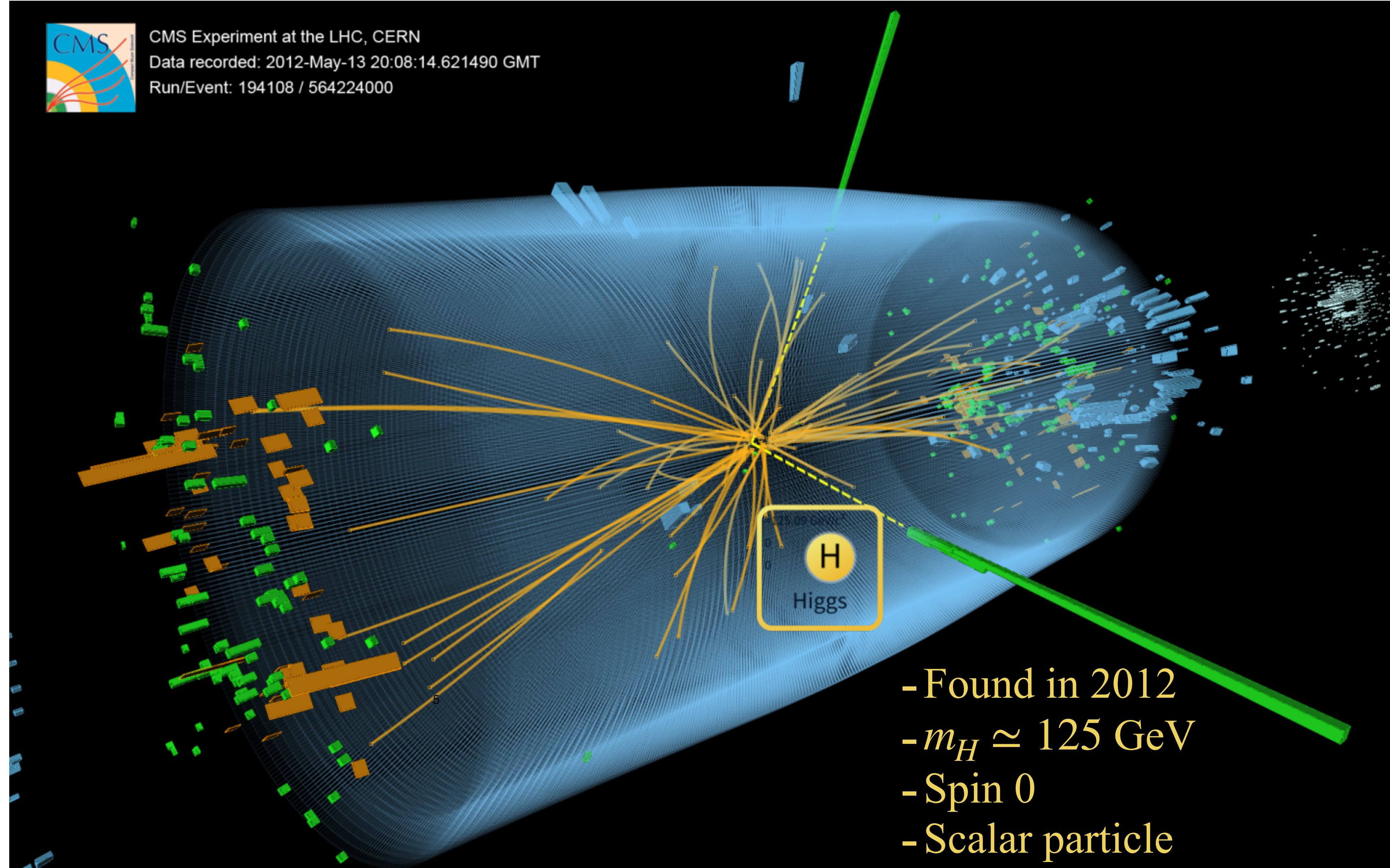
Outline

- Motivation: why composite Higgs?
- Lattice studies: our works and the chimera baryon
- Conclusion and outlook

Why composite Higgs?



CMS Experiment at the LHC, CERN
Data recorded: 2012-May-13 20:08:14.621490 GMT
Run/Event: 194108 / 564224000



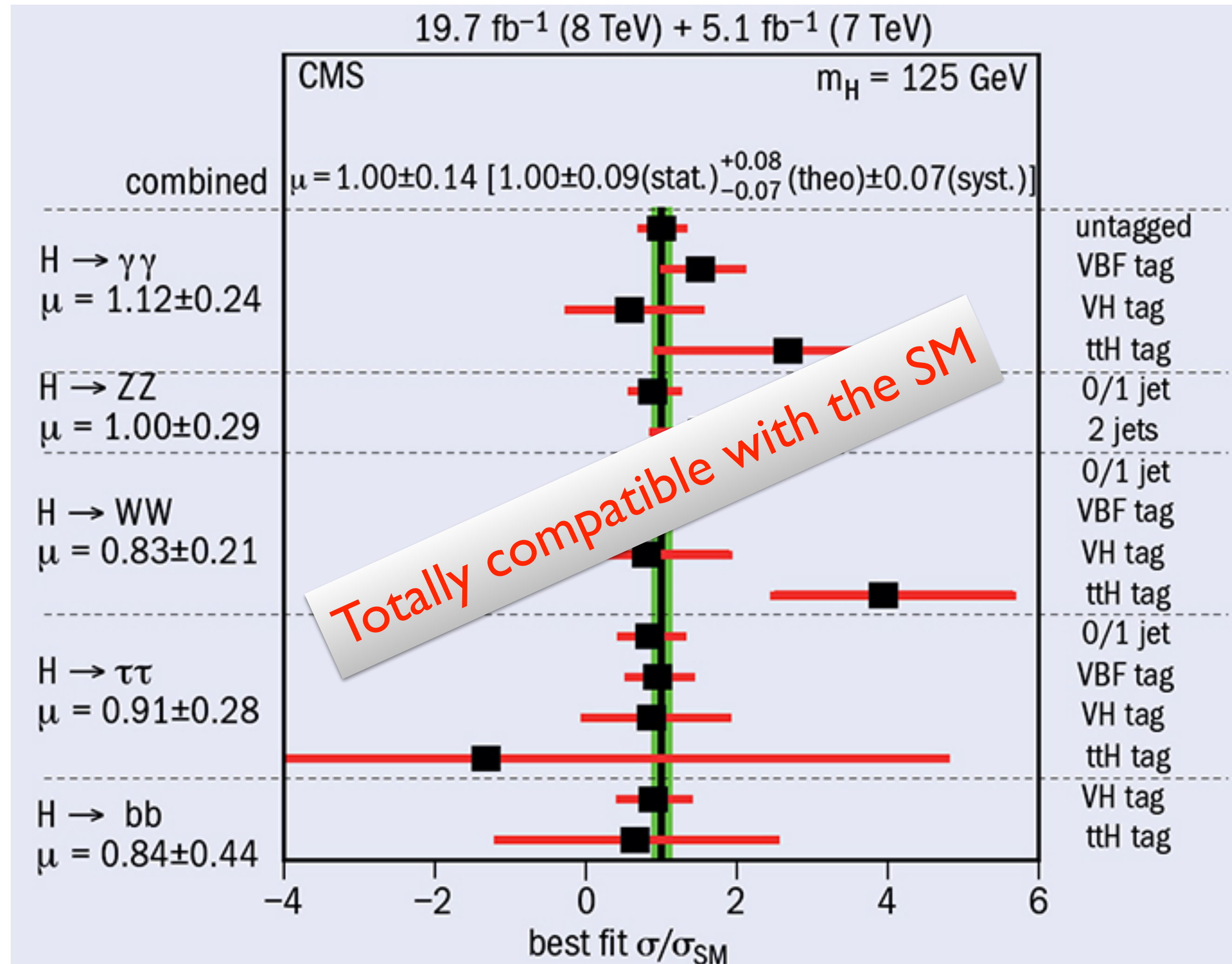
- Found in 2012
- $m_H \simeq 125$ GeV
- Spin 0
- Scalar particle

three generations of matter (fermions)				
	I	II	III	
mass	$\approx 2.4 \text{ MeV}/c^2$	$\approx 1.275 \text{ GeV}/c^2$	$\approx 172.44 \text{ GeV}/c^2$	$\approx 125.09 \text{ GeV}/c^2$
charge	$2/3$	$2/3$	$2/3$	0
spin	$1/2$	$1/2$	$1/2$	1
QUARKS	u up	c charm	t top	g gluon
	d down	s strange	b bottom	γ photon
	e electron	μ muon	τ tau	Z Z boson
LEPTONS	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson
				SCALAR BOSONS
				GAUGE BOSONS

triviality of the scalar sector

→ SM is an EFT

On the other hand...

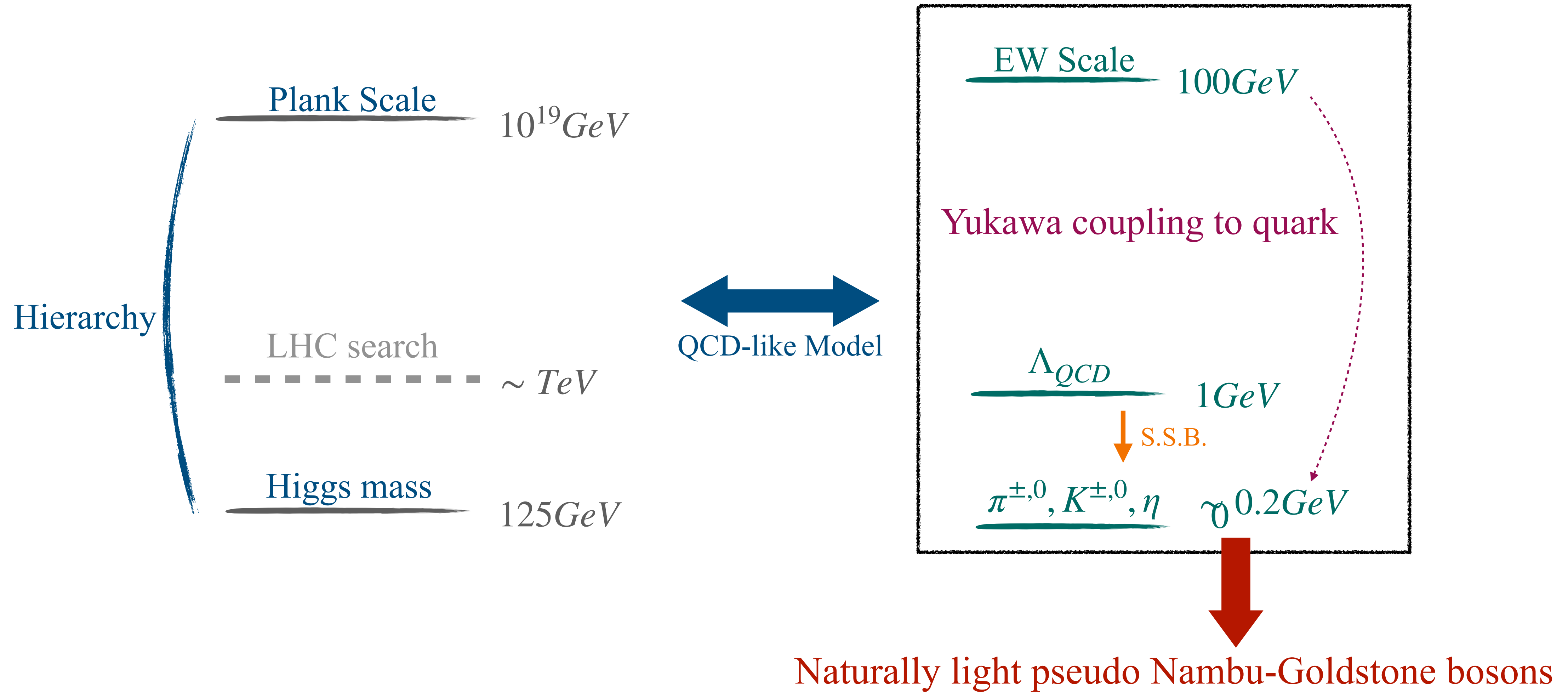


Searched up here ~10 TeV

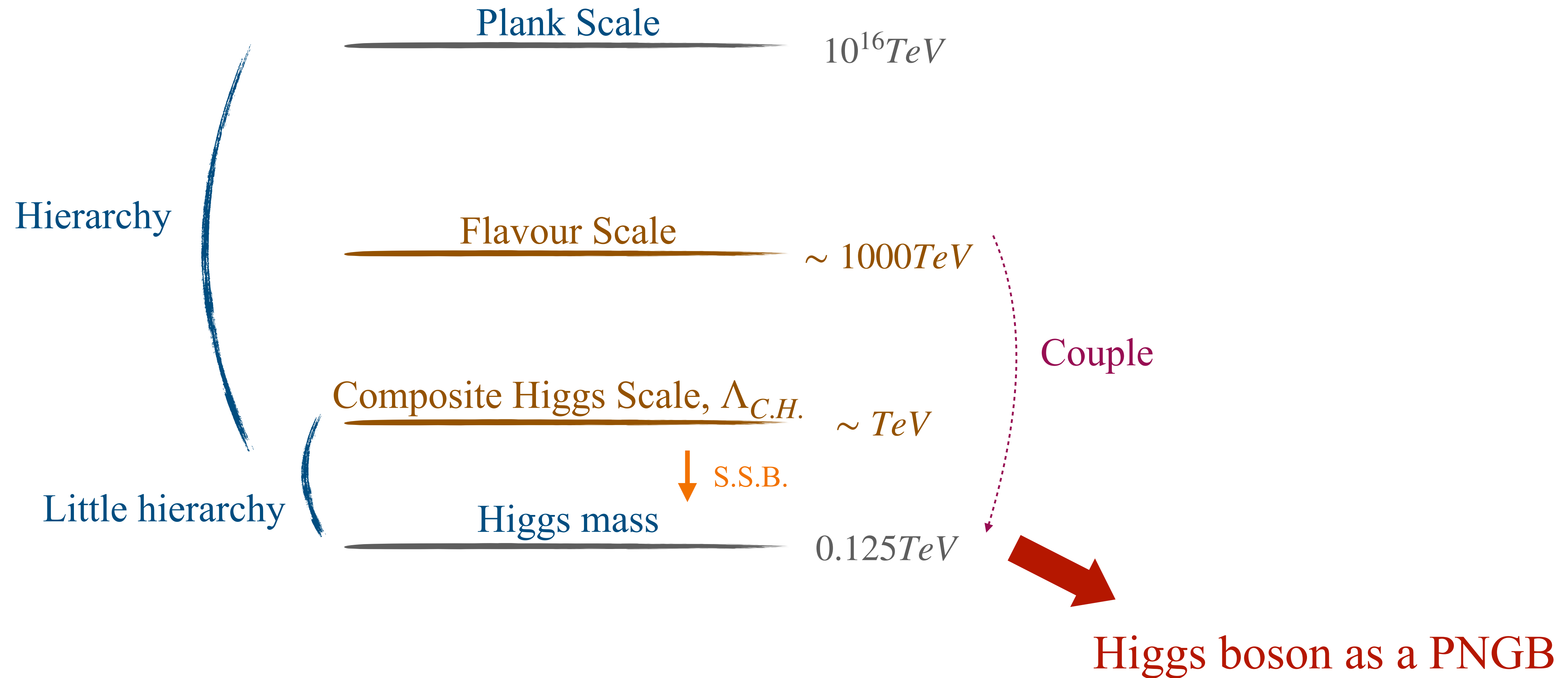
Higgs boson ~125 GeV

Why is the Higgs boson so light?

Lesson from QCD



Composite Higgs models: Hierarchy of scales



Composite Higgs models: Generic features

D.B. Kaplan, H. Georgi, M. Dugan, S. Dimopoulos,... *circa* 1985

- Global symmetry G broken to H
- Standard model global $G_W \subset H$
- The Higgs boson $\in G/H$
→ *c.f.*, technicolour where Higgs $\in H$
- Higgs mass generated *via* vacuum misalignment
→ $v \ll f \sin \langle \theta \rangle$, $f = |\vec{F}| \sim \Lambda_{HC}$
- Top-quark mass generated *via* partial compositeness
→ Spin-1/2 bound states mixing with top quark

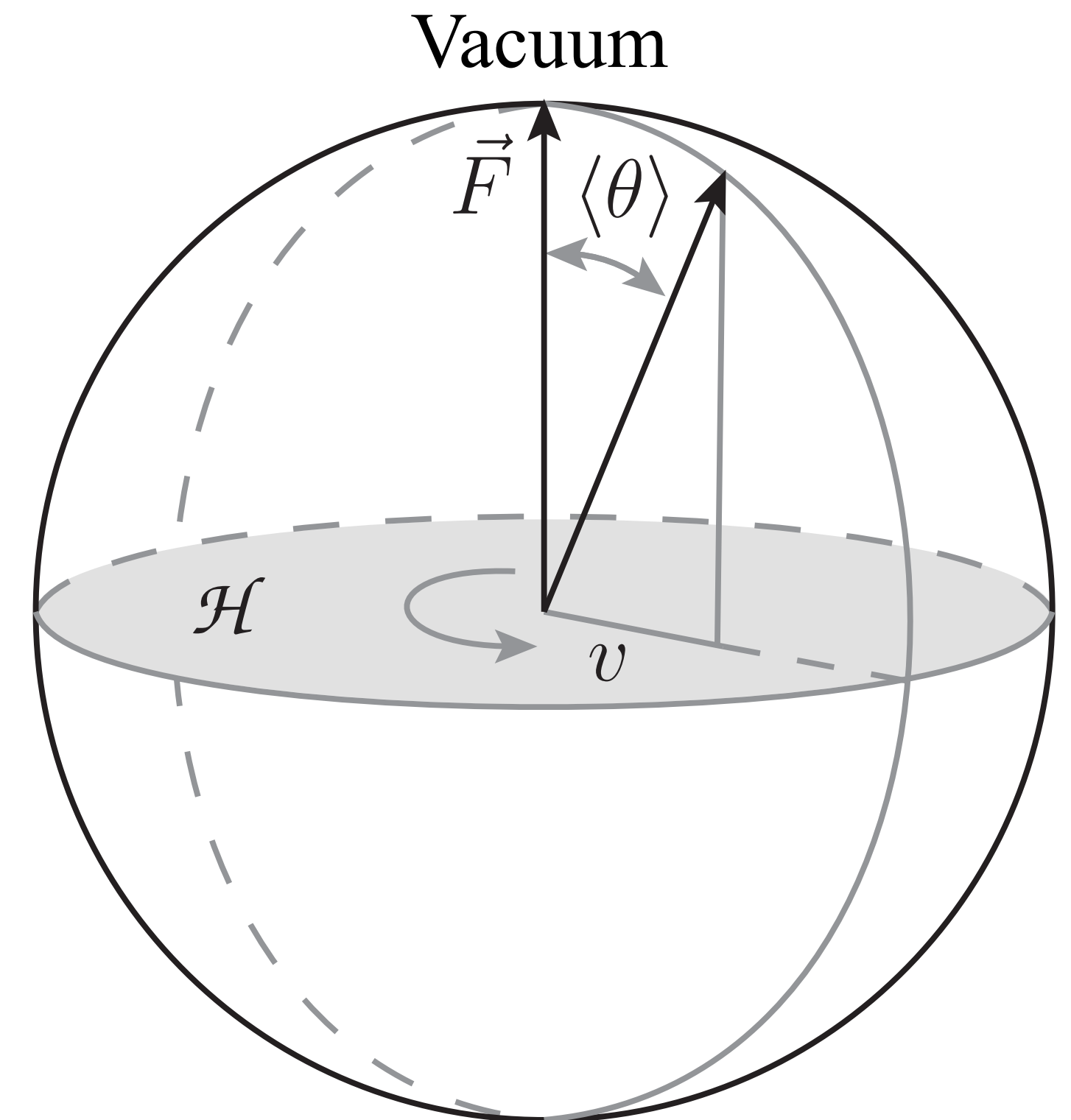


Figure from G. Panico and A. Wulzer, 1506.01961

D.B. Kaplan, 1991

UV completion of composite Higgs models

*Two-component relativistic fermions

Name	Gauge group	ψ	χ	Baryon type
M1	$SO(7)$	$5 \times \mathbf{F}$	$6 \times \mathbf{Spin}$	$\psi\chi\chi$
M2	$SO(9)$	$5 \times \mathbf{F}$	$6 \times \mathbf{Spin}$	$\psi\chi\chi$
M3	$SO(7)$	$5 \times \mathbf{Spin}$	$6 \times \mathbf{F}$	$\psi\psi\chi$
M4	$SO(9)$	$5 \times \mathbf{Spin}$	$6 \times \mathbf{F}$	$\psi\psi\chi$
M5	$Sp(4)$	$5 \times \mathbf{A}_2$	$6 \times \mathbf{F}$	$\psi\chi\chi$
M6	$SU(4)$	$5 \times \mathbf{A}_2$	$3 \times (\mathbf{F}, \bar{\mathbf{F}})$	$\psi\chi\chi$
M7	$SO(10)$	$5 \times \mathbf{F}$	$3 \times (\mathbf{Spin}, \bar{\mathbf{Spin}})$	$\psi\chi\chi$
M8	$Sp(4)$	$4 \times \mathbf{F}$	$6 \times \mathbf{A}_2$	$\psi\psi\chi$
M9	$SO(11)$	$4 \times \mathbf{Spin}$	$6 \times \mathbf{F}$	$\psi\psi\chi$
M10	$SO(10)$	$4 \times (\mathbf{Spin}, \bar{\mathbf{Spin}})$	$6 \times \mathbf{F}$	$\psi\psi\chi$
M11	$SU(4)$	$4 \times (\mathbf{F}, \bar{\mathbf{F}})$	$6 \times \mathbf{A}_2$	$\psi\psi\chi$
M12	$SU(5)$	$4 \times (\mathbf{F}, \bar{\mathbf{F}})$	$3 \times (\mathbf{A}_2, \bar{\mathbf{A}}_2)$	$\psi\psi\chi, \psi\chi\chi$

The minimal model

Barnard et al, arXiv:1311.6562

D. Franzosi and G. Ferretti, arXiv:1905.08273

Fermion representations and global symmetry

M. Peskin, 1980

For N_f flavours of Dirac fermions

Gauge group representation

Global symmetry breaking pattern

Complex

$$SU(N_f) \times SU(N_f) \rightarrow SU(N_f)$$

Real

$$SU(2N_f) \rightarrow SO(2N_f)$$

Pseudo-real

$$SU(2N_f) \rightarrow Sp(2N_f)$$

Our choice of model

- $Sp(4)$ gauge theory with $2\mathbf{F}+3\mathbf{AS}$ Dirac fermions



- Breaking pattern: $4\mathbf{F}+6\mathbf{AS}$ 2-component Weyl fermions

$$G/H = \underline{SU(4)} \times SU(6) / Sp(4) \times SO(6)$$

Enhanced global symmetry due to the (pseudo-) reality

● $SU(4)/Sp(4)$ gives 5 goldstone bosons.

- ▶ 4: SM Higgs doublet
- ▶ 1: made heavy in model building

● $SU(3)$ embedded in antisymmetric representation:

$$SU(6) \rightarrow SO(6) \supset SU(3)$$

└→ QCD colour $SU(3)$

The low-lying chimera baryon states

- Interpolating operators

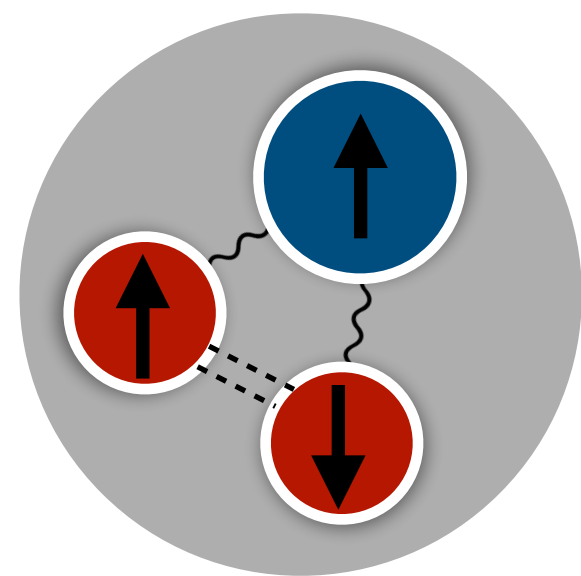
- Λ type: $\mathcal{O}_{\text{CB},\gamma^5} = (\bar{\psi}^1 a \gamma^5 \psi^2 b) \Omega_{bc} \chi^{k ca}$

a, b, c : hypercolour

Ω : 4×4 symplectic matrix

J : spin

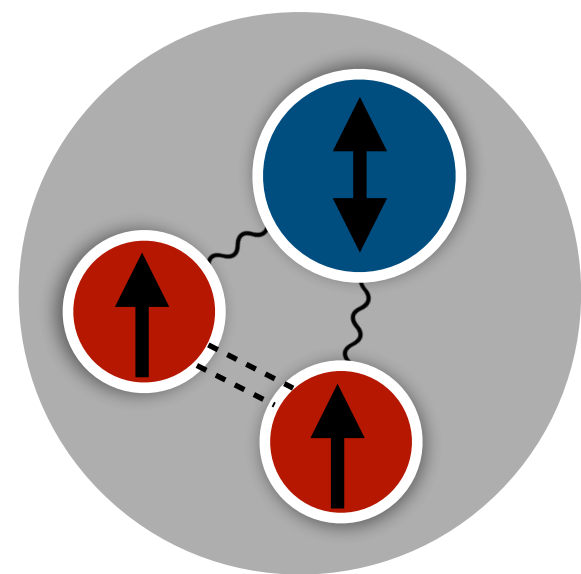
R : irreducible rep. of the fundamental sector



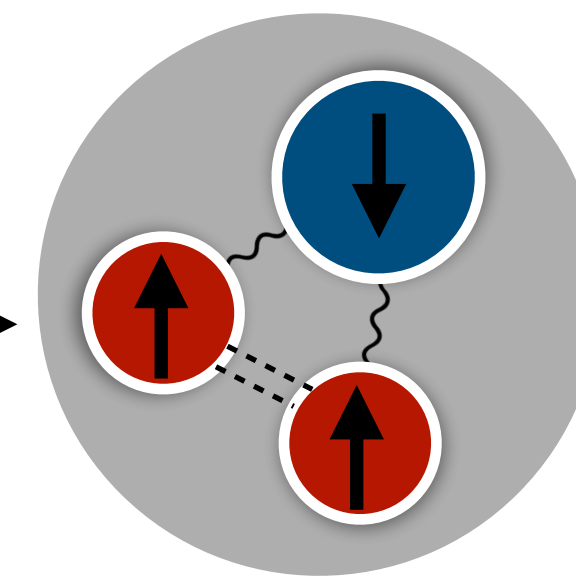
$(J, R) = (1/2, 5)$

*top partner

- Σ type: $\mathcal{O}_{\text{CB},\gamma^\mu} = (\bar{\psi}^1 a \gamma^\mu \psi^2 b) \Omega_{bc} \chi^{k ca}$

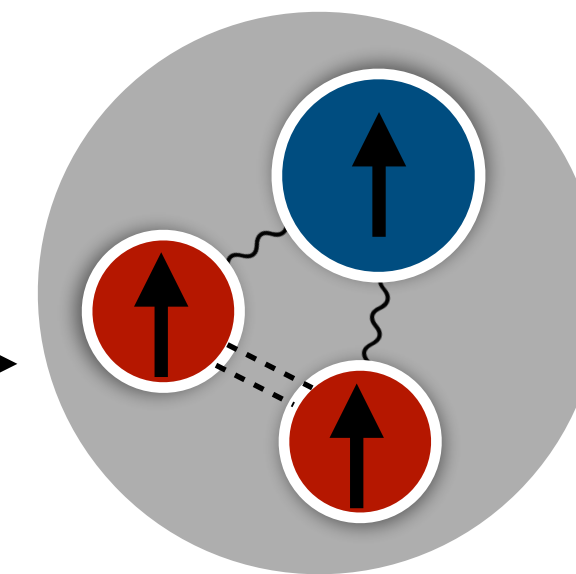


Spin projection



Σ : $(J, R) = (1/2, 10)$

*top partner



Σ^* : $(J, R) = (3/2, 10)$

$$m_{\text{top}} \sim 1/m_{\text{CB}}$$

Lattice studies

Major works from our collaboration

- Quenched fundamental mesons

JHEP 03 (2018) 185, arXiv:1712.04220

- $N_f = 2$ dynamical fundamental mesons

JHEP 12 (2019) 053, arXiv:1909.12662

- Quenched fundamental and antisymmetric mesons

Phys. Rev. D 101 (2020) 7, 074516, arXiv:1912.06505

- Quenched glueballs

Phys. Rev. D 103 (2021) 5, 054509, arXiv:2010.15781

- General features of $N_f = 2$ fundamental and $n_f = 3$ antisymmetric dynamical hyperquarks

Phys. Rev. D 106 (2022) 1, 014501, arXiv:2202.05516

- Quenched chimera baryons

Submitted to Phys. Rev. D, arXiv:2311.14663

Quenched chimera baryons

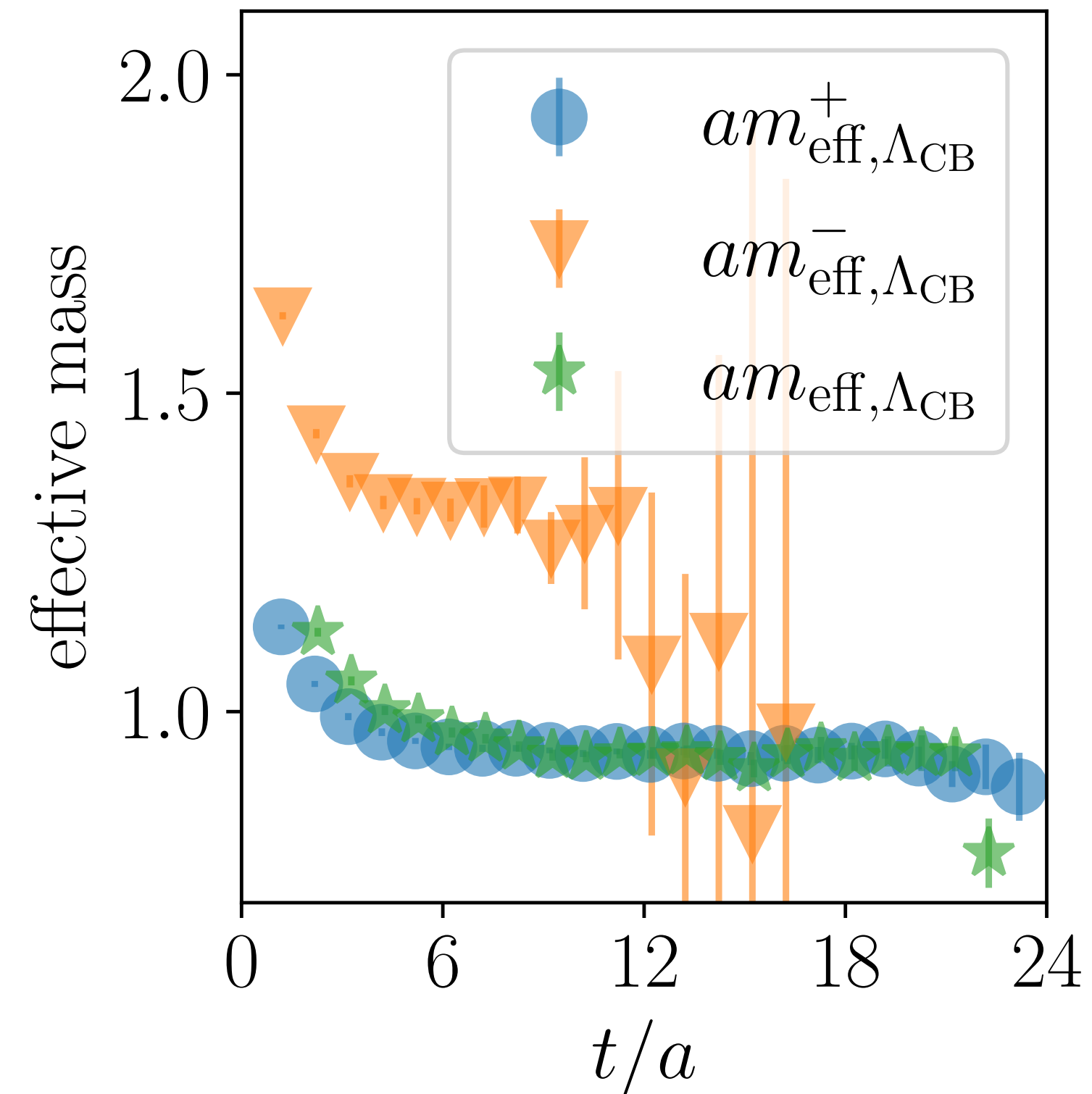
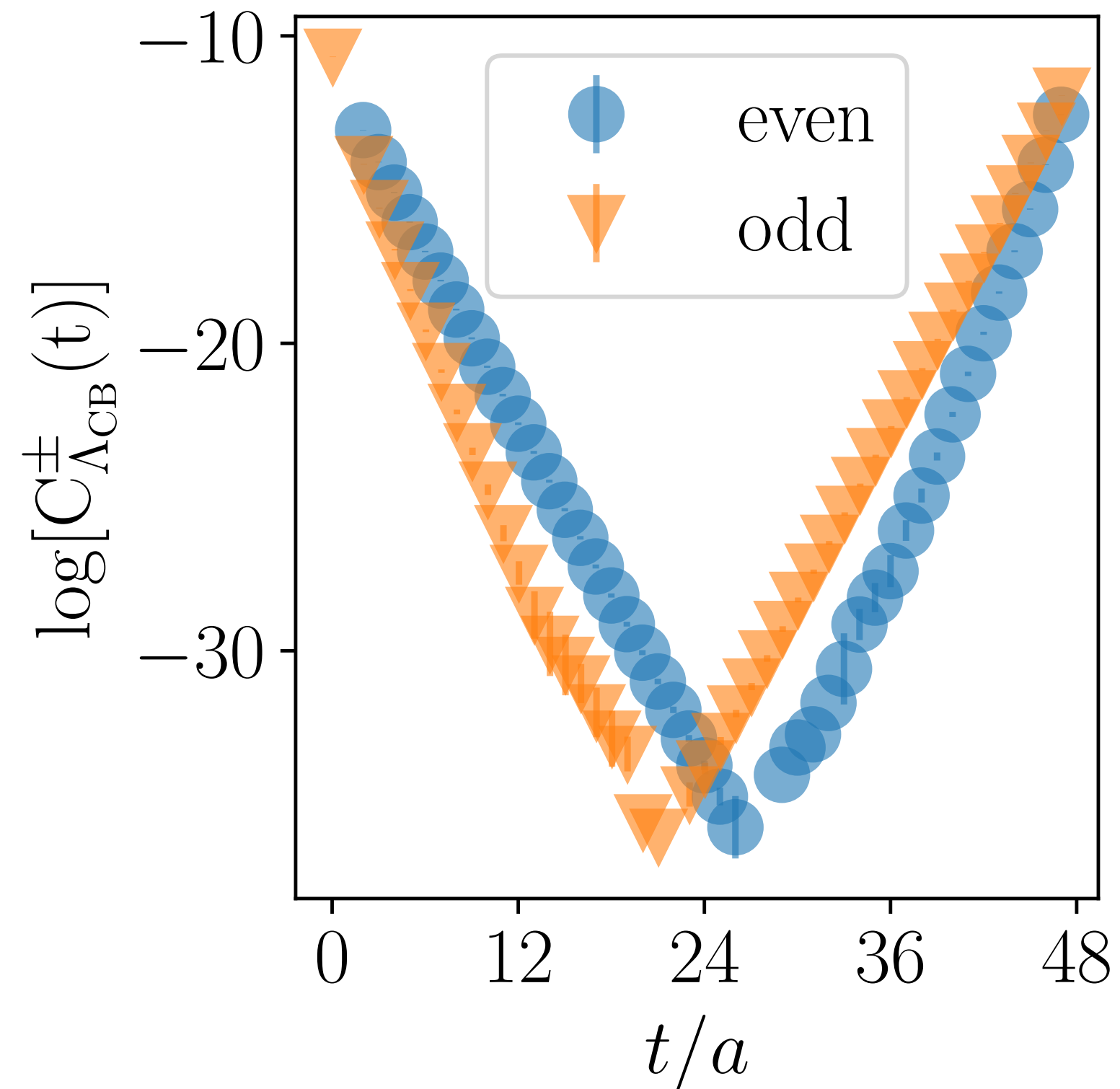
- Scan of parameter space
- Wilson plaquette and Wilson fermion actions

Ensemble	β	$N_t \times N_s^3$	$\langle P \rangle$	w_0/a
QB1	7.62	48×24^3	0.6018898(94)	1.448(3)
QB2	7.7	60×48^3	0.6088000(35)	1.6070(19)
QB3	7.85	60×48^3	0.6203809(28)	1.944(3)
QB4	8.0	60×48^3	0.6307425(27)	2.3149(12)
QB5	8.2	60×48^3	0.6432302(25)	2.8812(21)

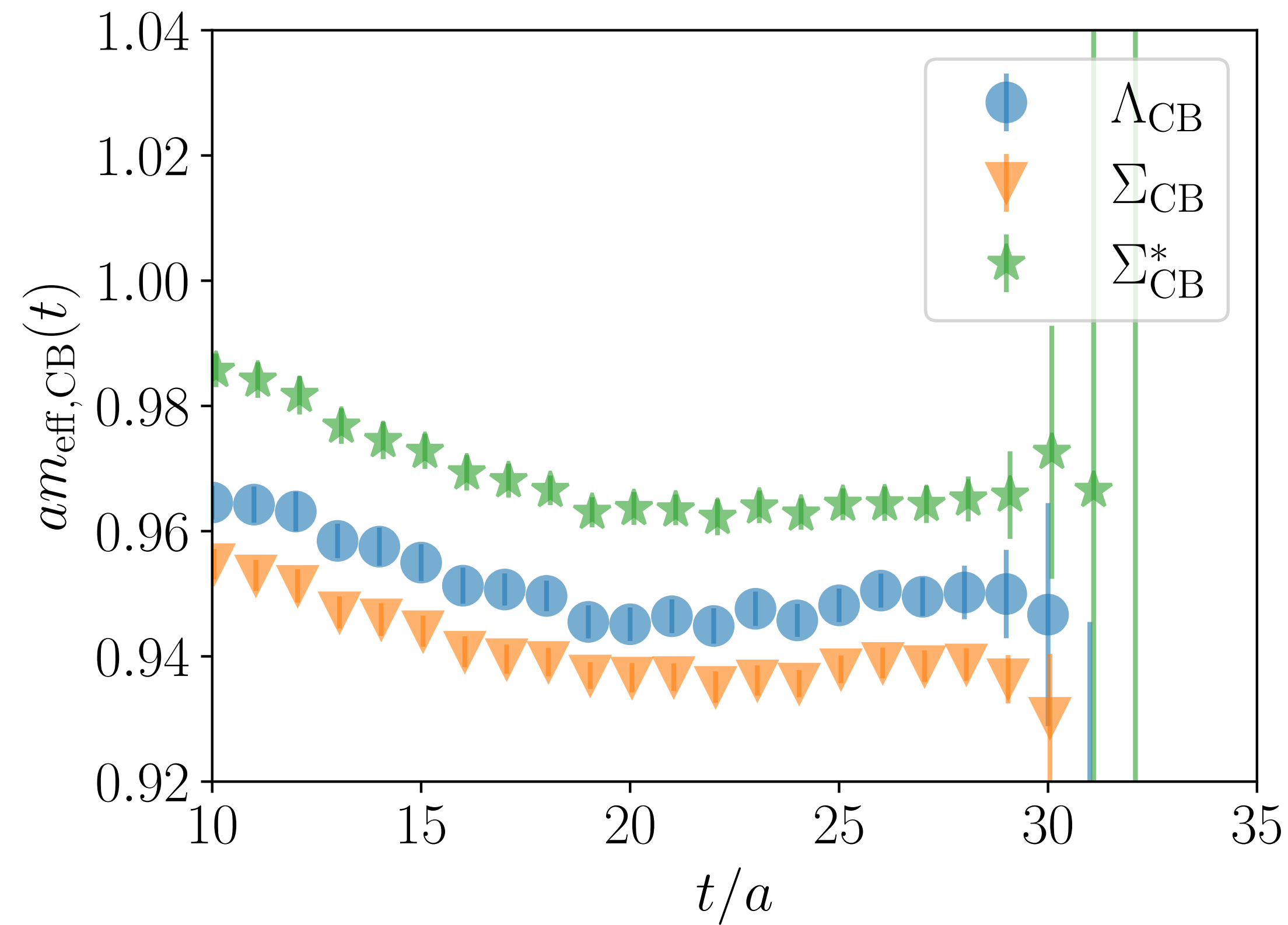
Parity partners: who is lighter?

$$C_{\text{CB}}(t) \xrightarrow{0 \ll t \ll T} P_+ \left[c_+ e^{-m^+ t} - c_- e^{-m^- (T-t)} \right] + P_- \left[c_- e^{-m^- t} - c_+ e^{-m^+ (T-t)} \right]$$

$$C_{\text{CB}}^\pm(t) \equiv P_\pm C_{\text{CB}}(t)$$

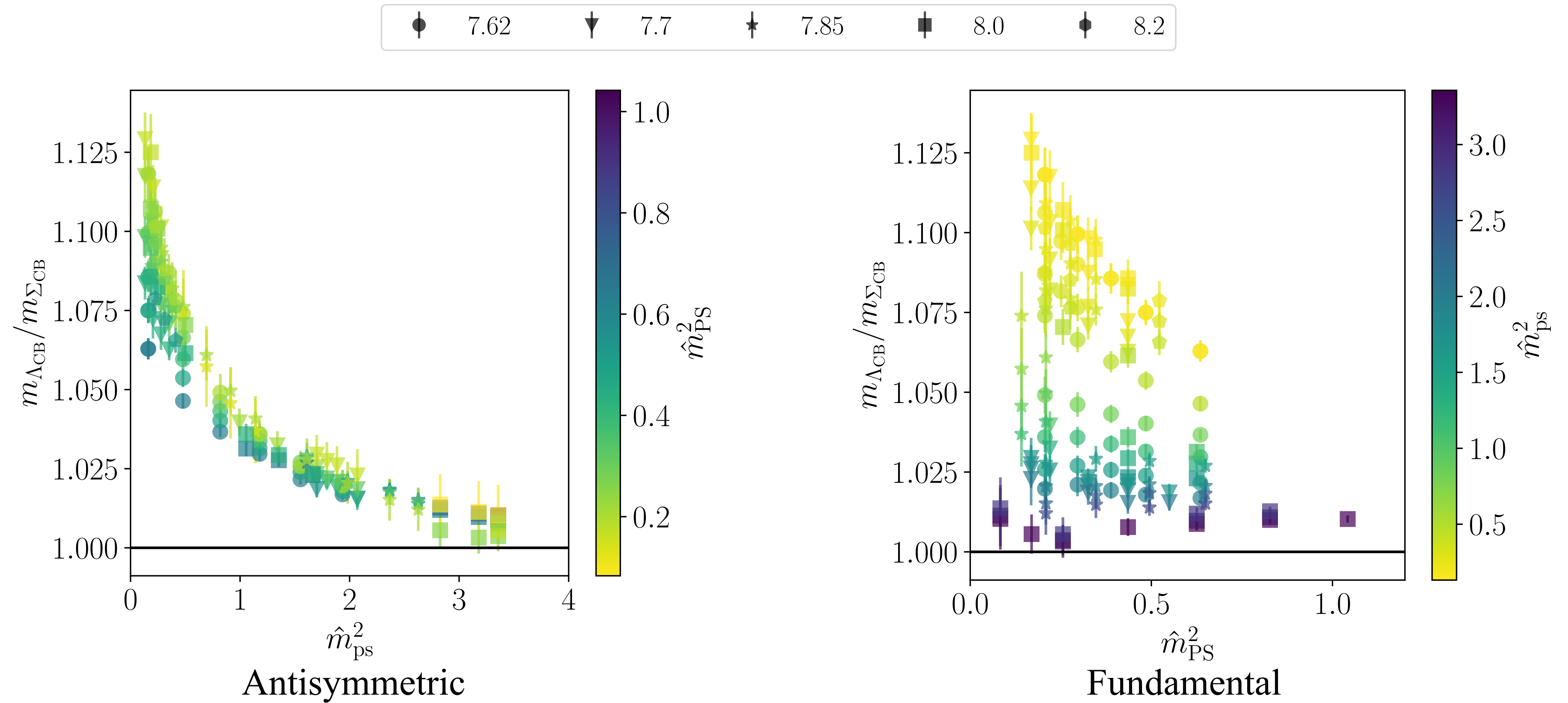


Typical mass hierarchy

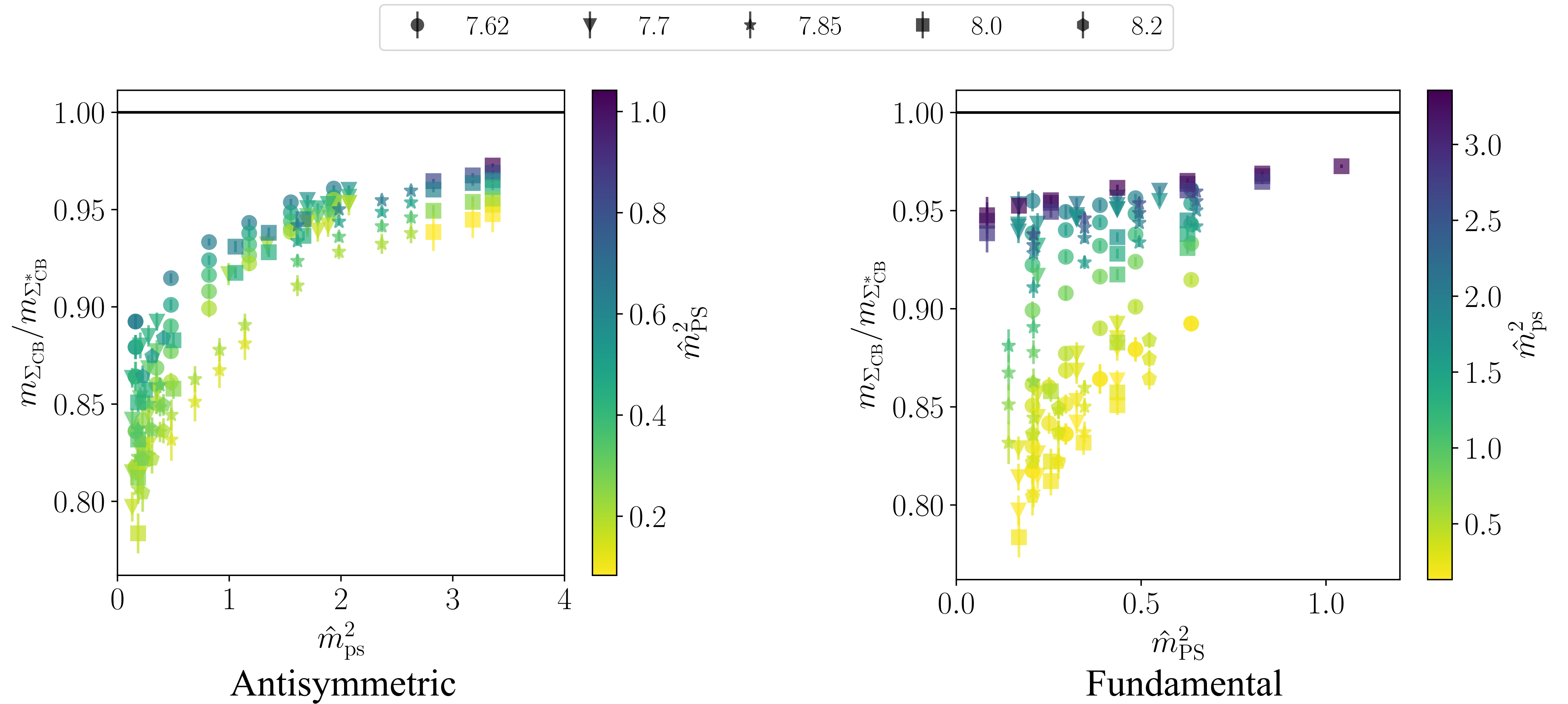


- Λ_{CB} is not lighter than Σ_{CB}
- *c.f.*, QCD where $m_{\Lambda} < m_{\Sigma}$

Typical mass hierarchy



Typical mass hierarchy

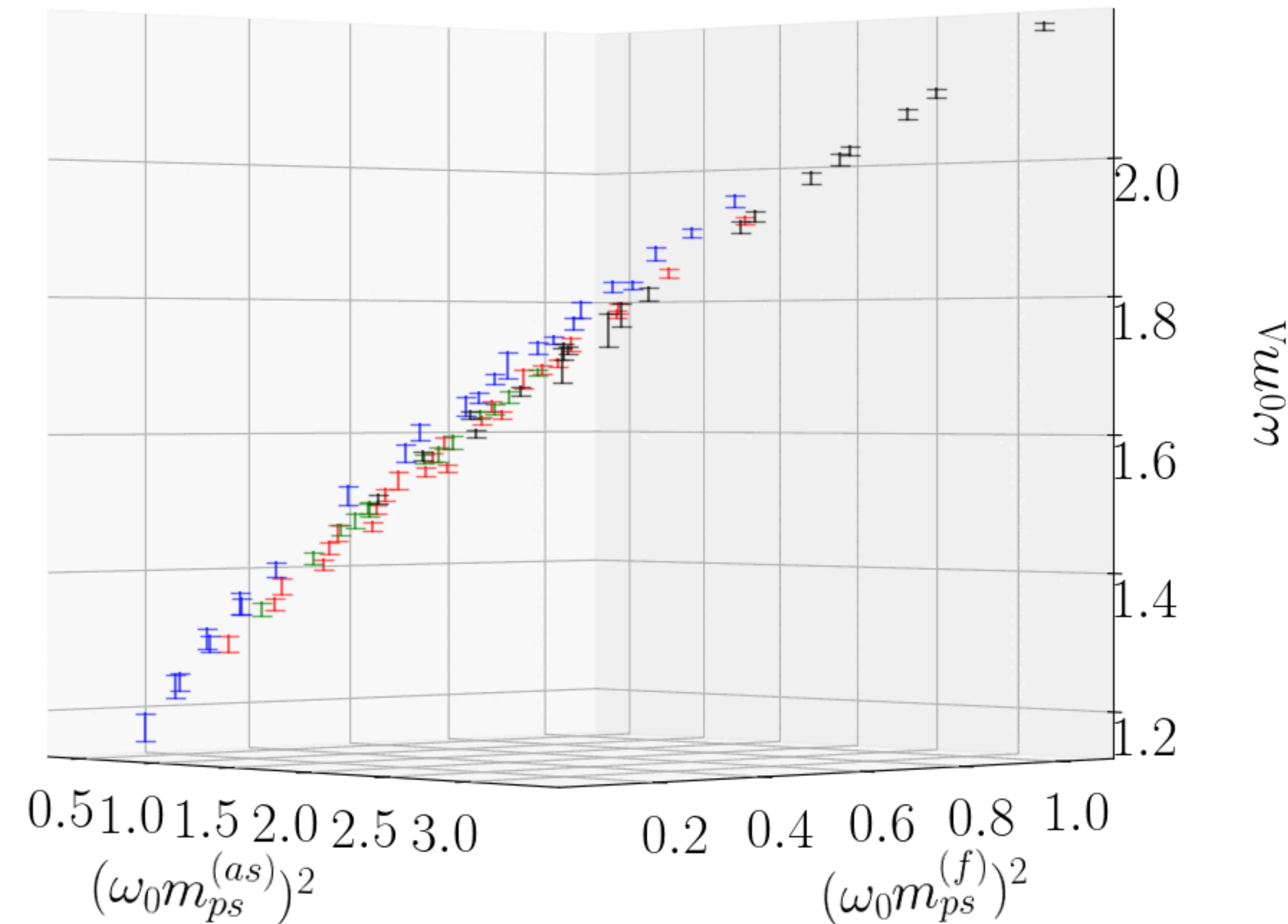


Hyperquark mass dependence

► Fit to analytic terms in baryon chiral perturbation theory

$$\begin{aligned}
 m_{\text{CB}} = & m_{\text{CB}}^{\chi} + F_2 \hat{m}_{\text{PS}}^2 + A_1 \hat{m}_{\text{ps}}^2 + L_1 \hat{a} \\
 & + F_3 \hat{m}_{\text{PS}}^3 + A_3 \hat{m}_{\text{ps}}^3 + L_{2F} \hat{a} \hat{m}_{\text{PS}}^2 + L_{2A} \hat{a} \hat{m}_{\text{ps}}^2 \\
 & + F_4 \hat{m}_{\text{PS}}^4 + A_4 \hat{m}_{\text{ps}}^4 + C_4 \hat{m}_{\text{PS}}^2 \hat{m}_{\text{ps}}^2
 \end{aligned}$$

- Cannot obtain stable fits
- Removing heavy-mass data does not help



Hyperquark mass dependence

► Fit to analytic terms in baryon chiral perturbation theory

$$\begin{aligned}
 m_{\text{CB}} = & \textcolor{red}{m}_{\text{CB}}^{\chi} + \textcolor{red}{F}_2 \hat{m}_{\text{PS}}^2 + \textcolor{blue}{A}_1 \hat{m}_{\text{ps}}^2 + \textcolor{red}{L}_1 \hat{a} & \text{---} & \text{---} & \text{---} & \text{---} & \text{---} & \text{---} & \text{---} & \text{---} & \text{M2} \\
 & + \textcolor{red}{F}_3 \hat{m}_{\text{PS}}^3 + \textcolor{red}{A}_3 \hat{m}_{\text{ps}}^3 + \textcolor{red}{L}_{2F} \hat{a} \hat{m}_{\text{PS}}^2 + \textcolor{red}{L}_{2A} \hat{a} \hat{m}_{\text{ps}}^2 & & & & & & & & \text{---} & \text{---} & \text{---} & \text{---} & \text{M3} \\
 & + \textcolor{red}{F}_4 \hat{m}_{\text{PS}}^4 + \textcolor{blue}{A}_4 \hat{m}_{\text{ps}}^4 + \textcolor{red}{C}_4 \hat{m}_{\text{PS}}^2 \hat{m}_{\text{ps}}^2 & & & & & & & & & & & & \\
 & \underbrace{\hspace{1.5cm}}_{\text{MF4}} & \underbrace{\hspace{1.5cm}}_{\text{MA4}} & \underbrace{\hspace{1.5cm}}_{\text{MC4}}
 \end{aligned}$$

Fit Ansatz	$\hat{m}_{\text{CB}}^{\chi}$	\hat{m}_{PS}^2	\hat{m}_{ps}^2	\hat{m}_{PS}^3	\hat{m}_{ps}^3	\hat{m}_{PS}^4	\hat{m}_{ps}^4	$\hat{m}_{\text{PS}}^2 \hat{m}_{\text{ps}}^2$	\hat{a}	$\hat{m}_{\text{PS}}^2 \hat{a}$	$\hat{m}_{\text{ps}}^2 \hat{a}$
M2	✓	✓	✓	-	-	-	-	-	✓	-	-
M3	✓	✓	✓	✓	✓	-	-	-	✓	✓	✓
MF4	✓	✓	✓	✓	✓	✓	-	-	✓	✓	✓
MA4	✓	✓	✓	✓	✓	-	✓	-	✓	✓	✓
MC4	✓	✓	✓	✓	✓	-	-	✓	✓	✓	✓

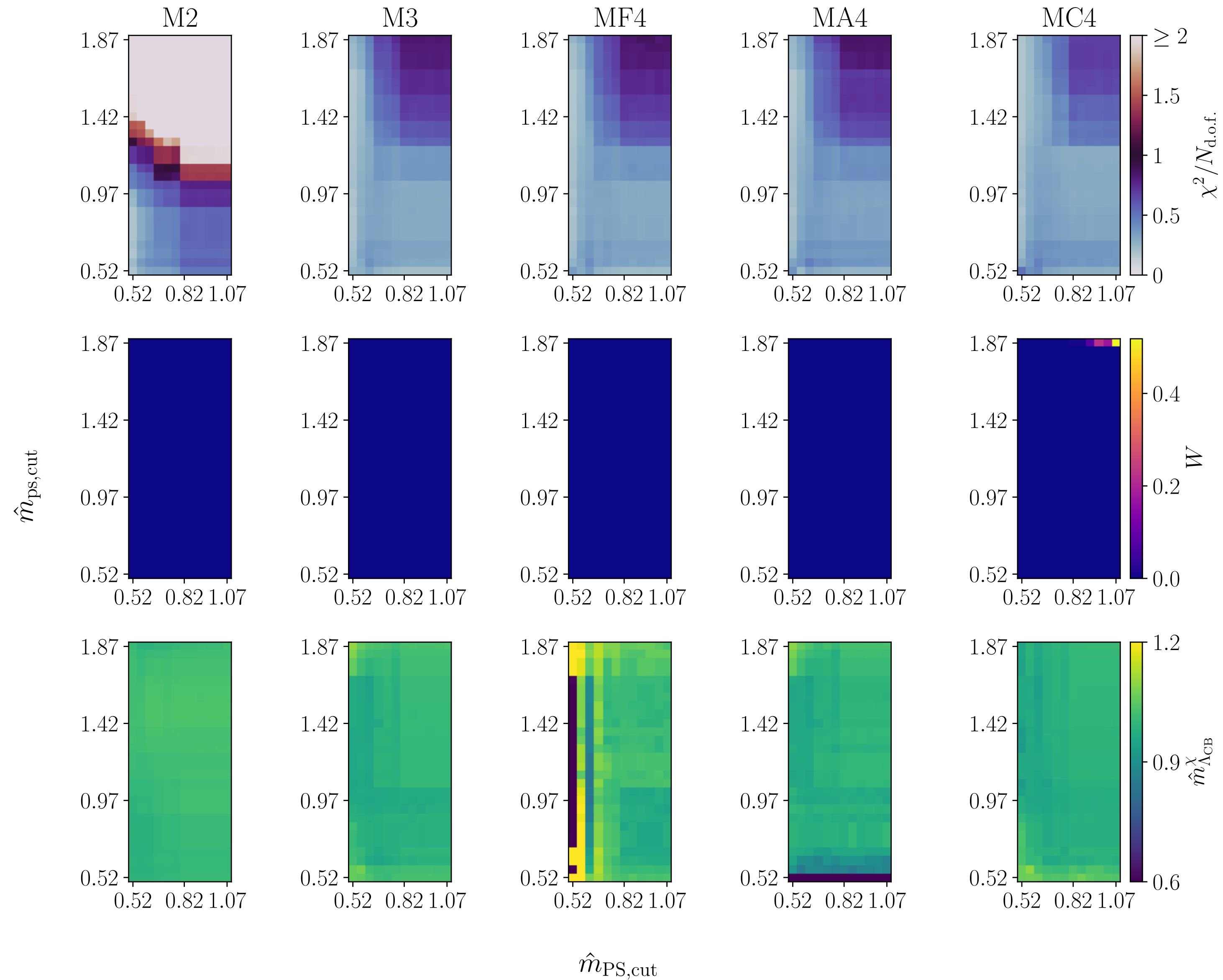
Procedures for the hyper quark-mass extrapolation

- Try the five fit ansatze
- Systematically include data points with $am_{\text{PS}} < 1$ and $am_{\text{ps}} < 1$
→ 263 data sets
- $263 \times 5 = 1315$ analysis procedures
- For each procedure, compute $\text{AIC} \equiv \chi^2 + 2k + 2N_{\text{cut}}$
of removed data points
of fit parameters
- Probability weight $W = \frac{1}{\mathcal{N}} \exp \left[-\frac{1}{2} \text{AIC} \right]$

Fit results for $m_{\Lambda_{\text{CB}}}$

► Polynomial terms in baryon chiral perturbation theory

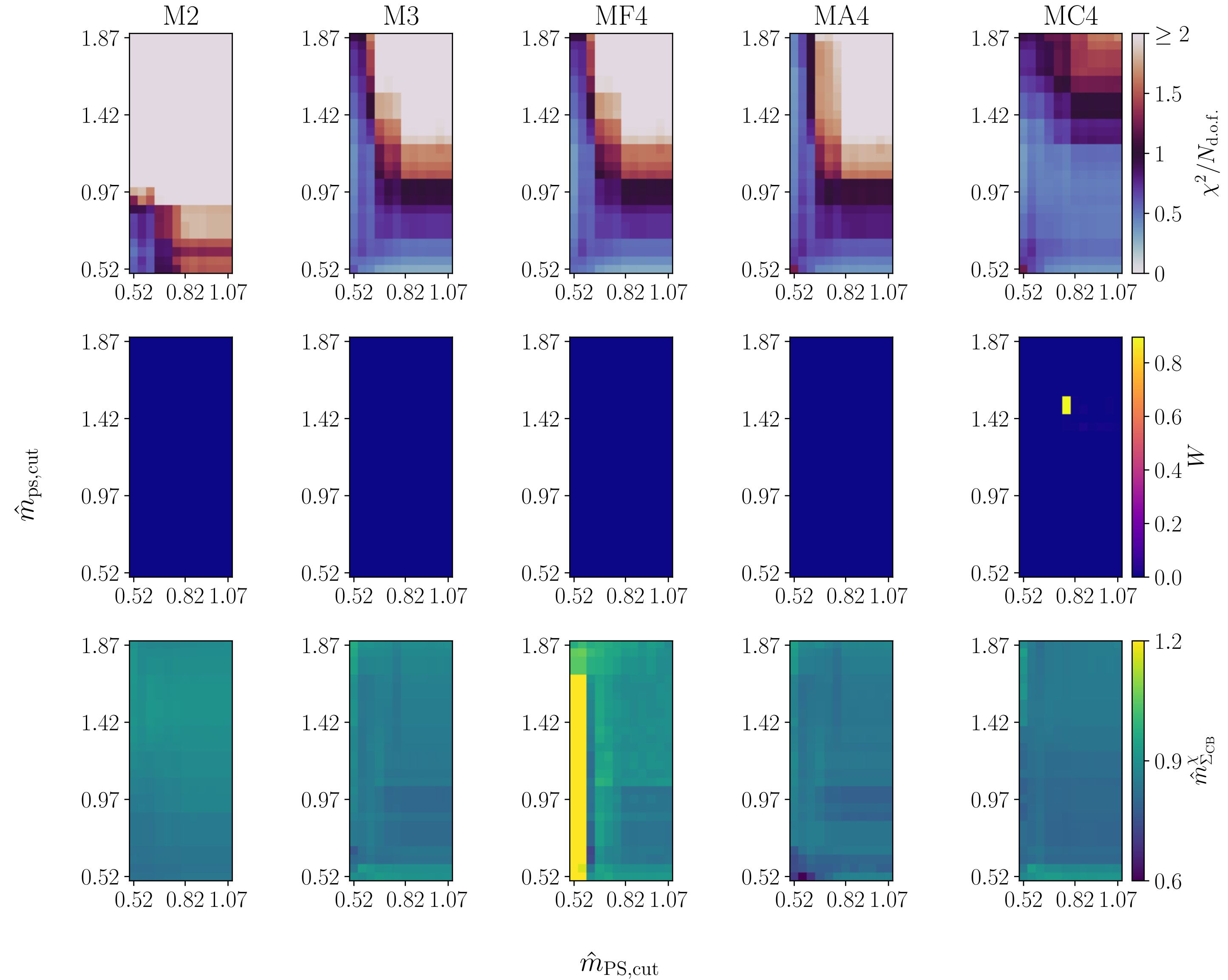
$$\begin{aligned}
 m_{\text{CB}} = & \textcolor{red}{m}_{\text{CB}}^{\chi} + \textcolor{red}{F}_2 \hat{m}_{\text{PS}}^2 + \textcolor{red}{A}_1 \hat{m}_{\text{ps}}^2 + \textcolor{red}{L}_1 \hat{a} \quad \text{--- M2} \\
 \text{M3 ---} & + \textcolor{red}{F}_3 \hat{m}_{\text{PS}}^3 + \textcolor{red}{A}_3 \hat{m}_{\text{ps}}^3 + \textcolor{red}{L}_{2F} \hat{a} \hat{m}_{\text{PS}}^2 + \textcolor{red}{L}_{2A} \hat{a} \hat{m}_{\text{ps}}^2 \\
 & + \textcolor{red}{F}_4 \hat{m}_{\text{PS}}^4 + \textcolor{red}{A}_4 \hat{m}_{\text{ps}}^4 + \textcolor{red}{C}_4 \hat{m}_{\text{PS}}^2 \hat{m}_{\text{ps}}^2 \\
 & \quad \text{MF4} \quad \text{MA4} \quad \text{M4C}
 \end{aligned}$$



Fit results for $m_{\Sigma_{\text{CB}}}$

► Polynomial terms in baryon chiral perturbation theory

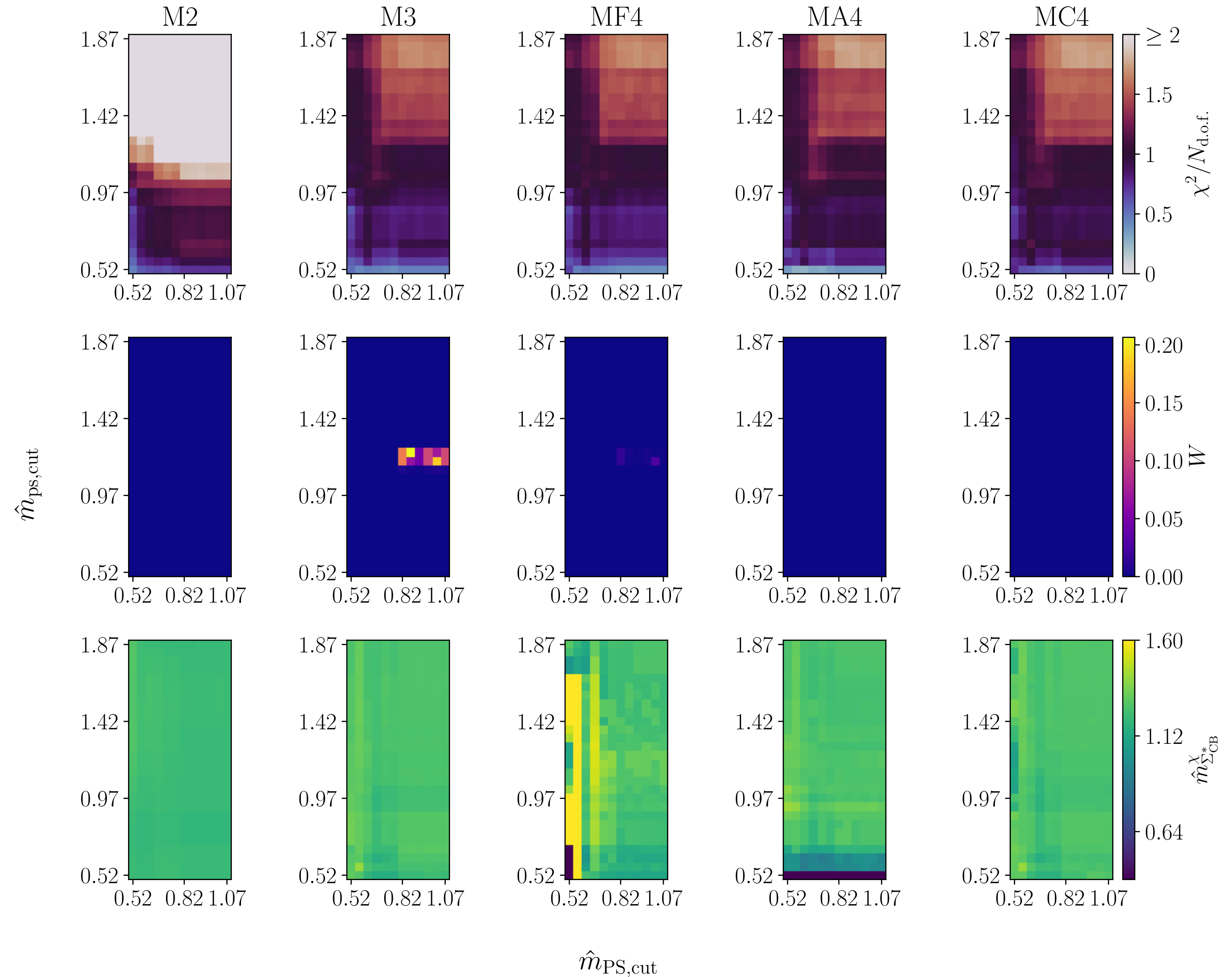
$$\begin{aligned}
 m_{\text{CB}} = & \color{red}{m}_{\text{CB}}^{\chi} + \color{red}{F}_2 \hat{m}_{\text{PS}}^2 + \color{red}{A}_1 \hat{m}_{\text{ps}}^2 + \color{red}{L}_1 \hat{a} \quad \text{--- M2} \\
 \text{M3} \quad & \text{---} \quad + \color{red}{F}_3 \hat{m}_{\text{PS}}^3 + \color{red}{A}_3 \hat{m}_{\text{ps}}^3 + \color{red}{L}_{2F} \hat{a} \hat{m}_{\text{PS}}^2 + \color{red}{L}_{2A} \hat{a} \hat{m}_{\text{ps}}^2 \\
 & + \color{red}{F}_4 \hat{m}_{\text{PS}}^4 + \color{red}{A}_4 \hat{m}_{\text{ps}}^4 + \color{red}{C}_4 \hat{m}_{\text{PS}}^2 \hat{m}_{\text{ps}}^2 \\
 & \quad \quad \quad \text{MF4} \quad \quad \text{MA4} \quad \quad \text{M4C}
 \end{aligned}$$



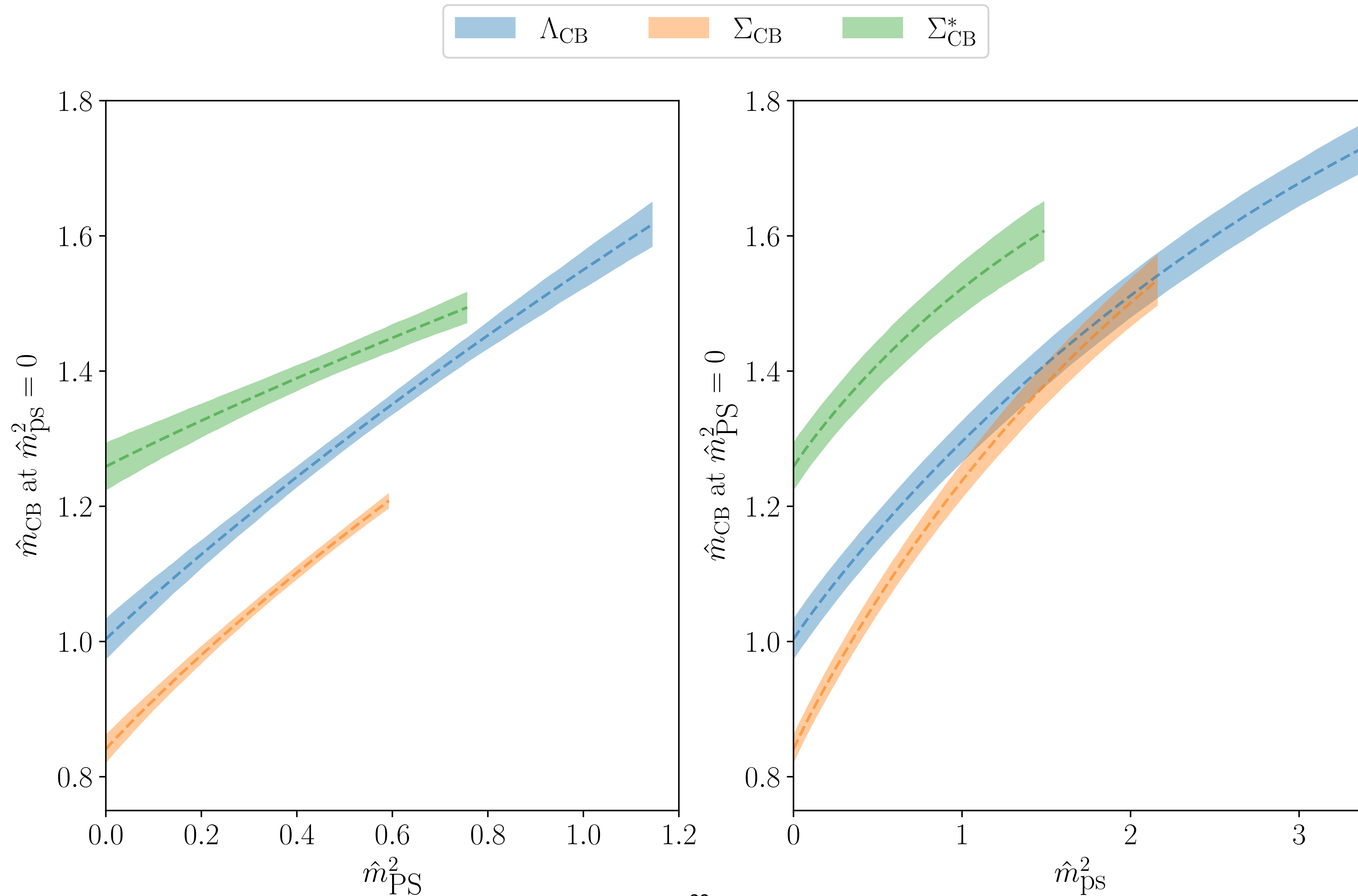
Fit results for $m_{\Sigma_{\text{CB}}^*}$

► Polynomial terms in baryon chiral perturbation theory

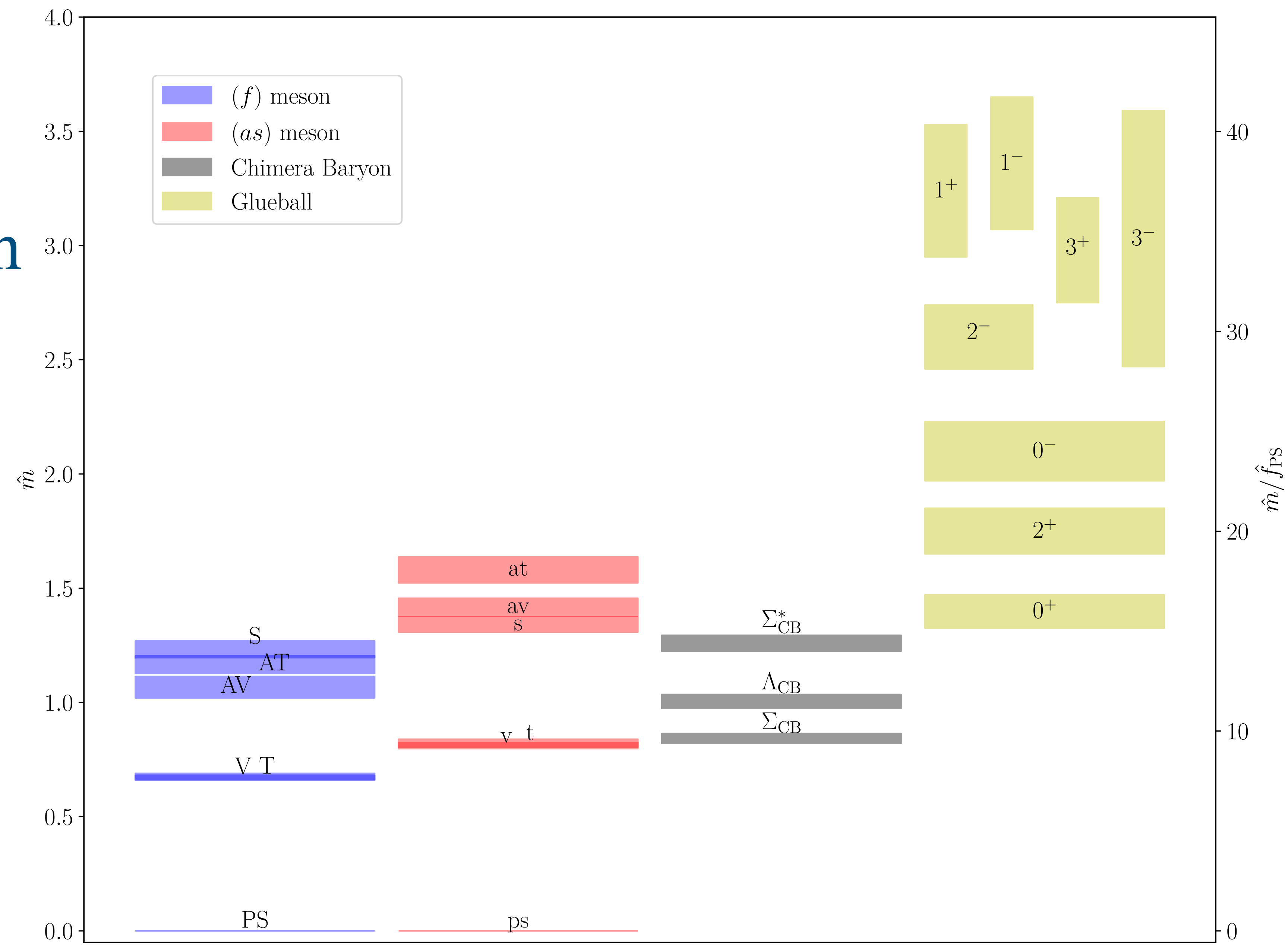
$$\begin{aligned}
 m_{\text{CB}} = & \color{red}{m}_{\text{CB}}^{\chi} + \color{red}{F}_2 \hat{m}_{\text{PS}}^2 + \color{red}{A}_1 \hat{m}_{\text{ps}}^2 + \color{red}{L}_1 \hat{a} \quad \text{--- M2} \\
 \text{M3} \quad & \text{---} \quad + \color{red}{F}_3 \hat{m}_{\text{PS}}^3 + \color{red}{A}_3 \hat{m}_{\text{ps}}^3 + \color{red}{L}_{2F} \hat{a} \hat{m}_{\text{PS}}^2 + \color{red}{L}_{2A} \hat{a} \hat{m}_{\text{ps}}^2 \\
 & \quad \quad \quad \underbrace{+ \color{red}{F}_4 \hat{m}_{\text{PS}}^4}_{\text{MF4}} + \underbrace{\color{red}{A}_4 \hat{m}_{\text{ps}}^4}_{\text{MA4}} + \underbrace{\color{red}{C}_4 \hat{m}_{\text{PS}}^2 \hat{m}_{\text{ps}}^2}_{\text{M4C}}
 \end{aligned}$$



Hyperquark-mass dependence



Quenched spectrum



Conclusion and outlook

- First lattice study of the chimera baryon masses in the $\text{Sp}(4)$ gauge theory
 → Key difference from QCD: Λ_{CB} may not be lighter than Σ_{CB}
- Fully-dynamical simulations in progress
- Mixing strength with the top quark, also large anomalous dimension
- Also in the $\text{Sp}(4)$ gauge theory: the Higgs potential

Backup slides

Gauge group repn and global coset

M. Peskin, 1980

★ Real : $(T^a)^* = (T^a)^T = -S^{-1} T^a S, \quad SS^* = 1.$

★ Pseudoreal : $(T^a)^* = (T^a)^T = -S^{-1} T^a S, \quad SS^* = -1.$

$$\Psi = \begin{pmatrix} \Psi_L \\ \Psi_R \end{pmatrix} \equiv \begin{pmatrix} \psi_\alpha \\ \bar{\chi}^{\dot{\beta}} \end{pmatrix} = \begin{pmatrix} \psi_\alpha \\ (\chi^\beta)^* \end{pmatrix}, \quad \bar{\Psi} \Psi = \epsilon^{\alpha\beta} \chi_\beta^{ia} \psi_{\alpha ia} + \text{h.c.}$$

gauge repn

condensate

global symmetry

Complex

$$\epsilon^{\alpha\beta} \psi_\beta^{i(\bar{r})} \psi_{\alpha i}^{(r)} + \text{h.c.}$$

$$SU(N_f) \times SU(N_f) \rightarrow SU(N_f)$$

Real

$$\epsilon^{\alpha\beta} \psi_\beta^{ia} \psi_{\alpha i}^b S_{ab}^{-1}$$

$$SU(2N_f) \rightarrow SO(2N_f)$$

Pseudoreal

$$\epsilon^{\alpha\beta} \psi_\beta^{ia} \psi_\alpha^{jb} S_{ab}^{-1} E_{ij}$$

$$SU(2N_f) \rightarrow Sp(2N_f)$$

The top partner and the top mass

$$\Psi_{ij}^{\alpha} = (\psi_i \chi^{\alpha} \psi_j), \quad \Psi_{ij}^{c,\alpha} = (\psi_i \chi^{c,\alpha} \psi_j)$$

$$\mathcal{L}^{\text{mix}} = -\frac{1}{2} \left\{ \lambda_1 M_* \left(\frac{M_*}{\Lambda} \right)^{d_{\Psi}-5/2} \Psi_1^T \tilde{C} t^c + \lambda_2 M_* \left(\frac{M_*}{\Lambda} \right)^{d_{\Psi^c}-5/2} t^T \tilde{C} \Psi_2^c + \right. \\ \left. + \lambda M_* \left[\Psi_1^T \tilde{C} \Psi_1^c + \Psi_2^T \tilde{C} \Psi_2^c \right] + y v_W \left[\Psi_1^T \tilde{C} \Psi_2^c + \Psi_2^T \tilde{C} \Psi_1^c \right] \right\} + \text{h.c.}$$

$$m_t^2 \simeq \frac{\lambda_1^2 \lambda_2^2 y^2 \left(\frac{M_*}{\Lambda} \right)^{2d_{\Psi}+2d_{\Psi^c}-10} v_W^2 M_*^4}{m_1^2 m_2^2} \quad \text{where} \quad m_1^2 \simeq \left(\lambda^2 + \lambda_1^2 \left(\frac{M_*}{\Lambda} \right)^{2d_{\Psi}-5} \right) M_*^2, \\ m_2^2 \simeq \left(\lambda^2 + \lambda_2^2 \left(\frac{M_*}{\Lambda} \right)^{2d_{\Psi^c}-5} \right) M_*^2$$

- ★ Need $d_{\Psi} = d_{\Psi^c} < 5/2$, ie, large anomalous dimension
 - ➔ IR conformality with more fermion flavours?
- ★ These couplings can be important for Higgs potential
 - ➔ Four-fermion operators

Composite Higgs with $Sp(4)$ gauge group

J. Barnard, T. Gherghetta, T.S. Ray, 2014

Field	$Sp(4)$ gauge	$SU(4)$ global
A_μ	10	1
ψ	4	4

- ★ Two Dirac fermions in the fundamental repn pseudoreal
- ★ The Higgs doublet in the coset $SU(4)/Sp(4)$
- ★ The SM $SU(2)_L \times SU(2)_R$ in the unbroken global $Sp(4)$